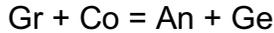


Example Using the Clausius-Clapeyron Equation

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Consider the reaction between grossular, corundum, anorthite and gehlenite:



Boettcher (1970) determined that this reaction takes place between 760 and 780 °C at 1 Kbar pressure.

Use Boettcher's results as a starting point and apply the Clausius-Clapeyron Equation to determine the temperature of reaction at 10 Kbar.

To do this:

This is a solid-solid reaction, so it is reasonable to assume that $\Delta S/\Delta V$ of reaction is about constant. So we can calculate the slope of the reaction at 1 bar and use that to extrapolate.

From thermodynamic reference books, we find the following 1-bar molar entropy and volume values for the four phases involved:

	SV	
	J/deg	Cm ³
Gr	255.5	125.3
Co	50.92	25.575
An	199.3	100.79
Ge	209.8	90.24

From these values we can calculate the ΔV and ΔS of reaction:

$$\Delta V = V_{\text{An}} + V_{\text{Ge}} - V_{\text{Gr}} - V_{\text{Co}} = 100.79 + 90.24 - 125.3 - 25.575 = 40.155 \text{ Cm}^3/\text{mol}$$

$$\Delta S = S_{\text{An}} + S_{\text{Ge}} - S_{\text{Gr}} - S_{\text{Co}} = 199.3 + 209.8 - 255.5 - 50.92 = 102.68 \text{ J/deg}\cdot\text{mol}$$

We need a conversion factor to help with the units:

$$10 \text{ Cm}^3 = 1 \text{ J/bar}$$

$$\text{So, } \Delta V = 4.0155 \text{ J/mol}$$

The Clausius-Clapeyron equation says that:

$$dP/dT = \Delta S / \Delta V = 102.68 / 4.0155 = 25.57 \text{ bar/deg}$$

Using this value, we find that if the reaction takes place at 770 °C at 1 Kbar, it must take place at 1121 °C at 10 Kbar.

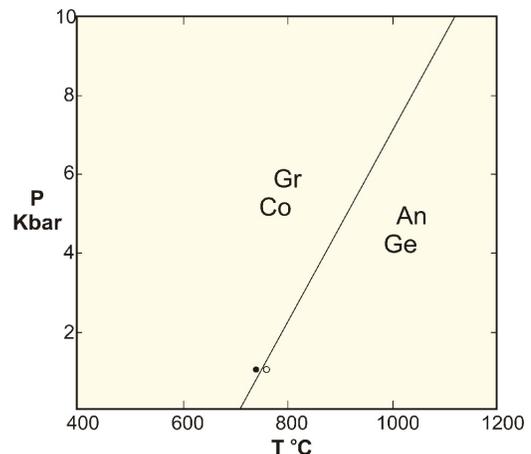


Figure 1. The reaction $\text{Gr}+\text{Co}=\text{An}+\text{Ge}$ extracted from Boettcher's (1970) experimental results (solid and open circles) to 10 Kbar.