

Applied Statistics: Linear Equations

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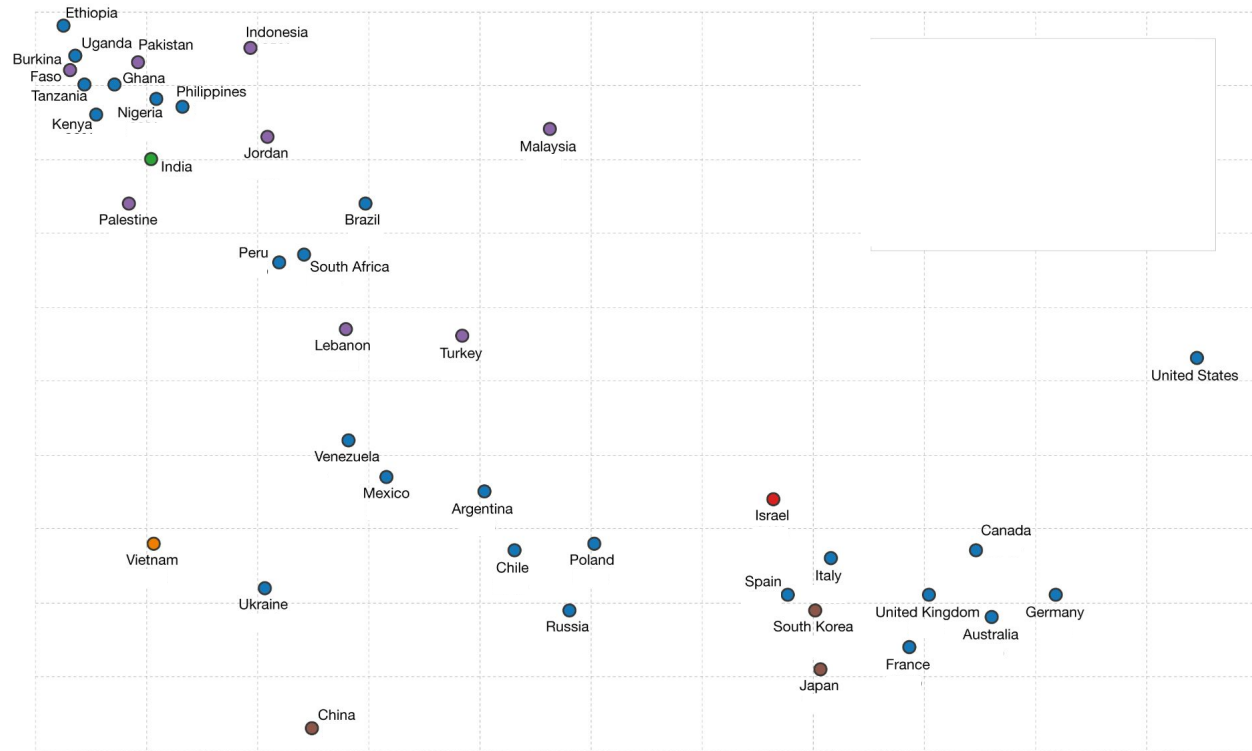
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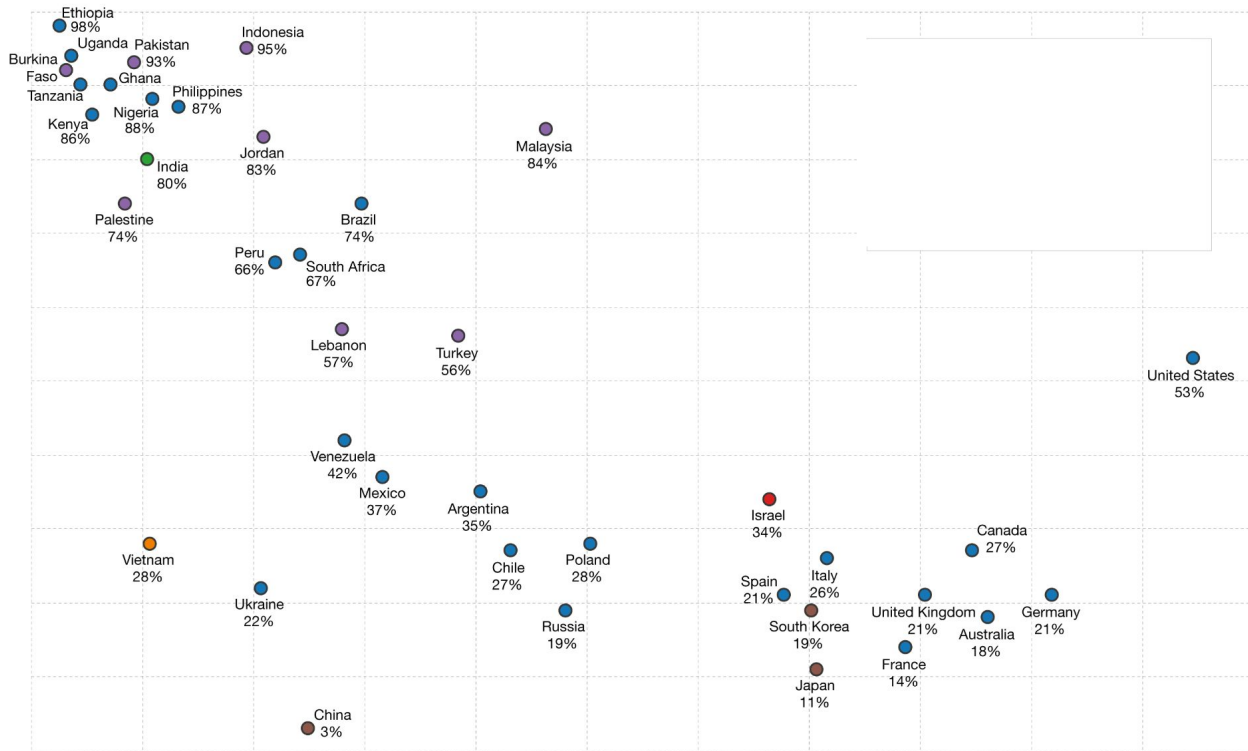
Plan for Today

- What's Upcoming
- Graph discussion
- Linear equations
- Individual activity

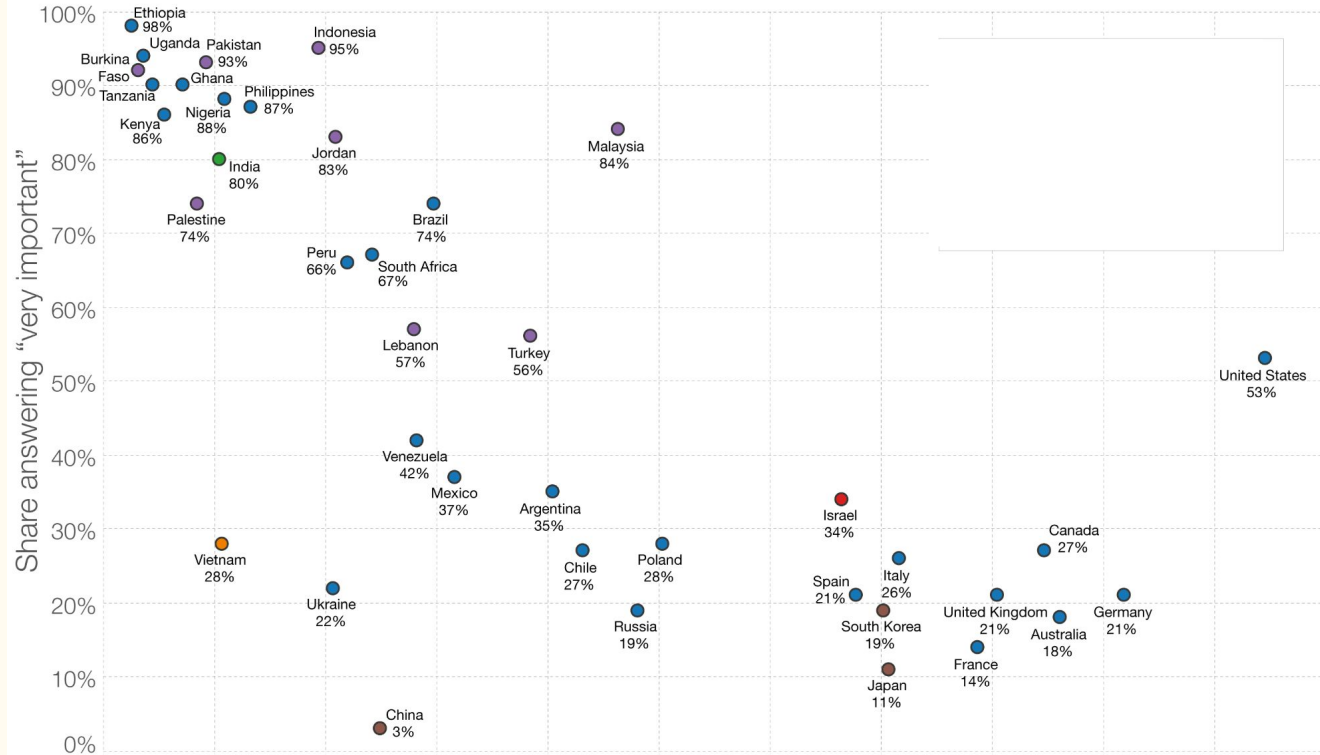
What's Upcoming/Ongoing

- Week 11 Homework – due Sunday.
- Daily Survey 30 – due Sunday.
- Checkpoint 3 – due Monday night.
- Reading Assignment 4 Writeup – due Wednesday, April 13th.
 - If you've already done 3 RA writeups, no need to do this!
- Project 2 – due Wednesday, April 20th.

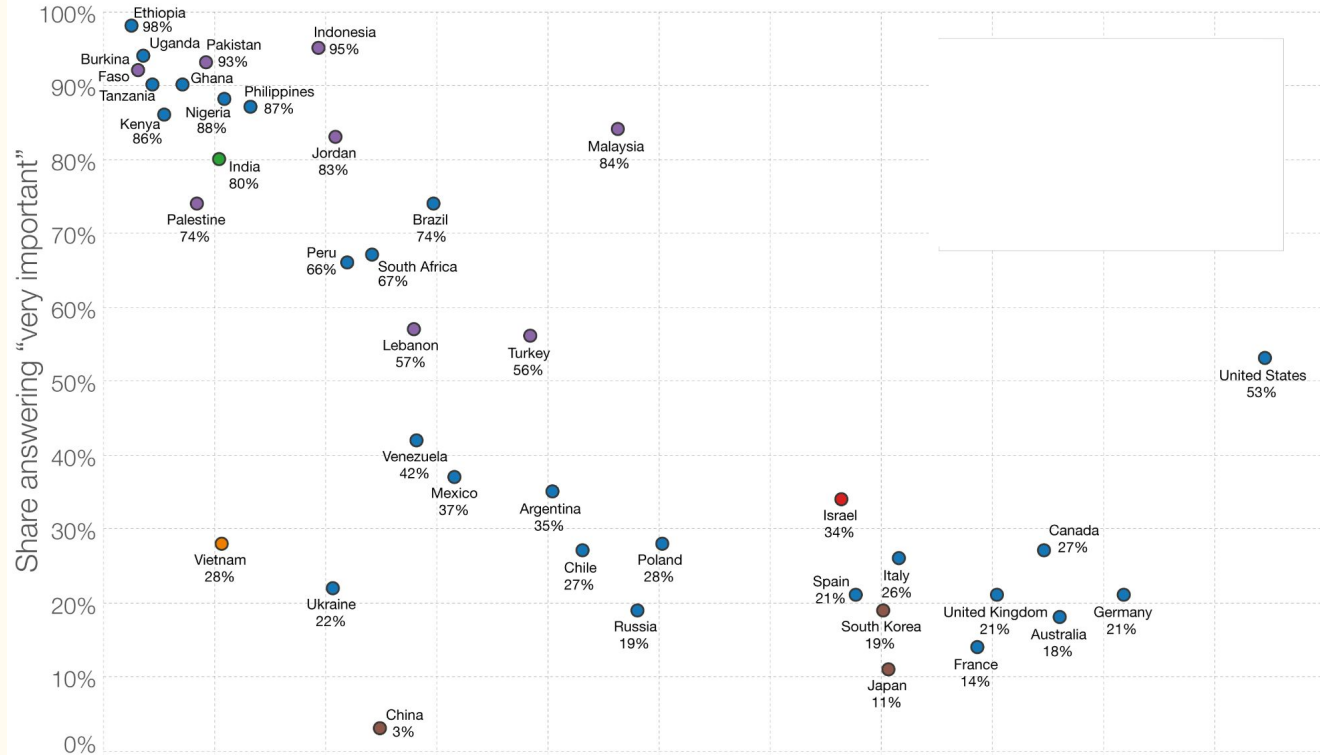




Importance of Religion vs

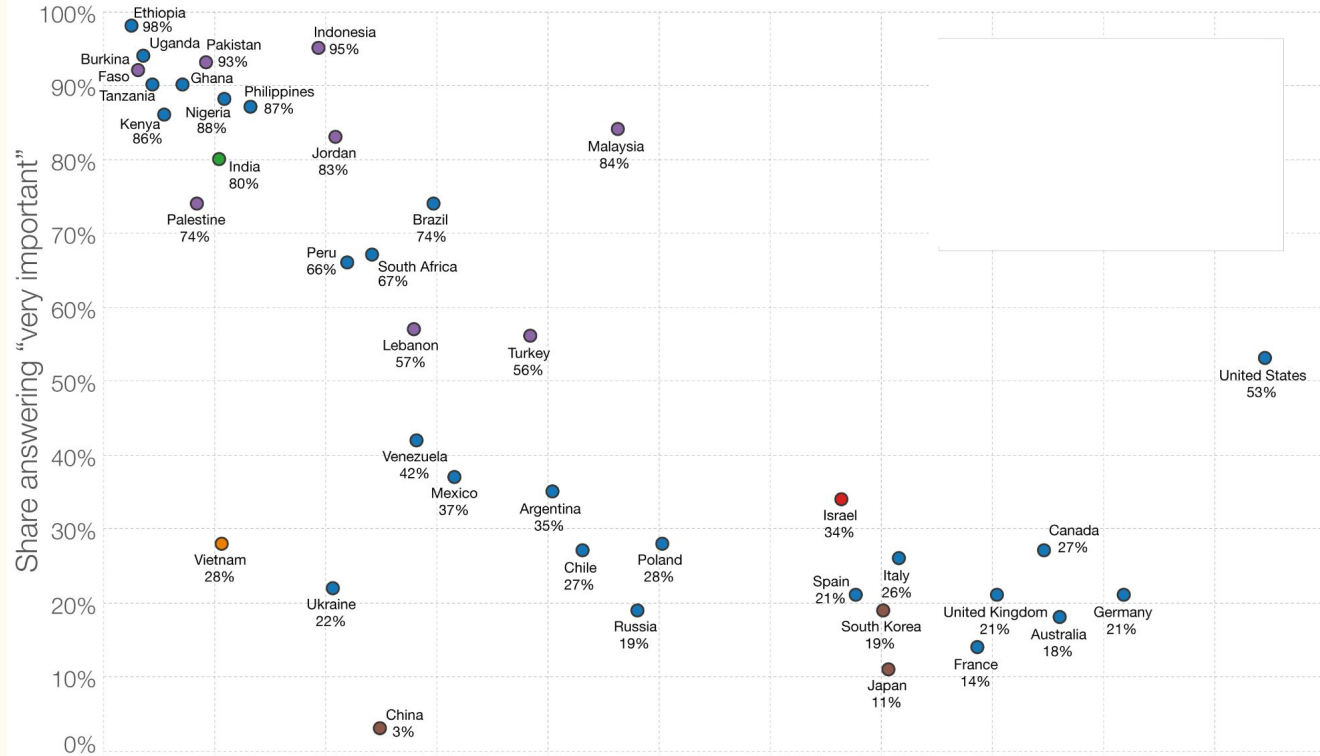


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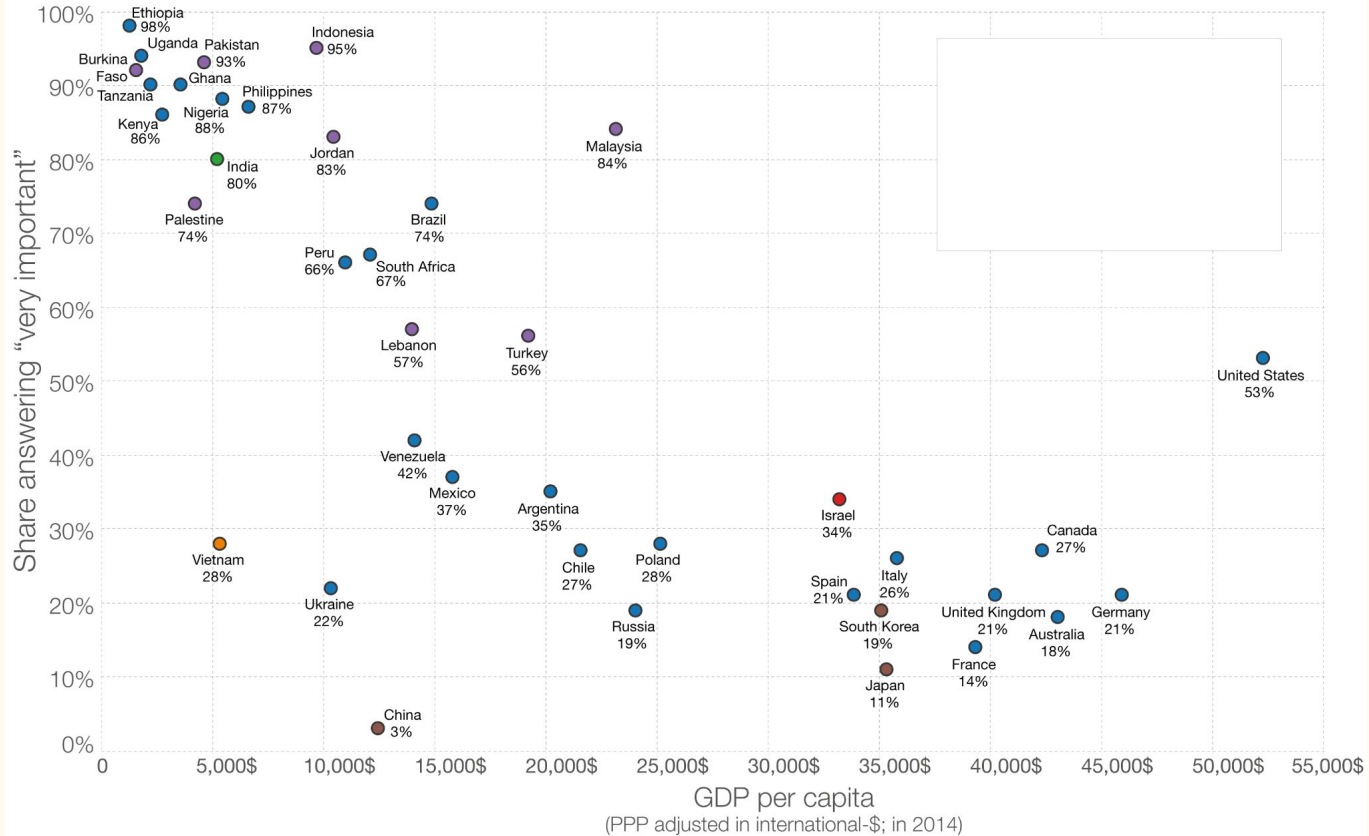


Importance of Religion vs

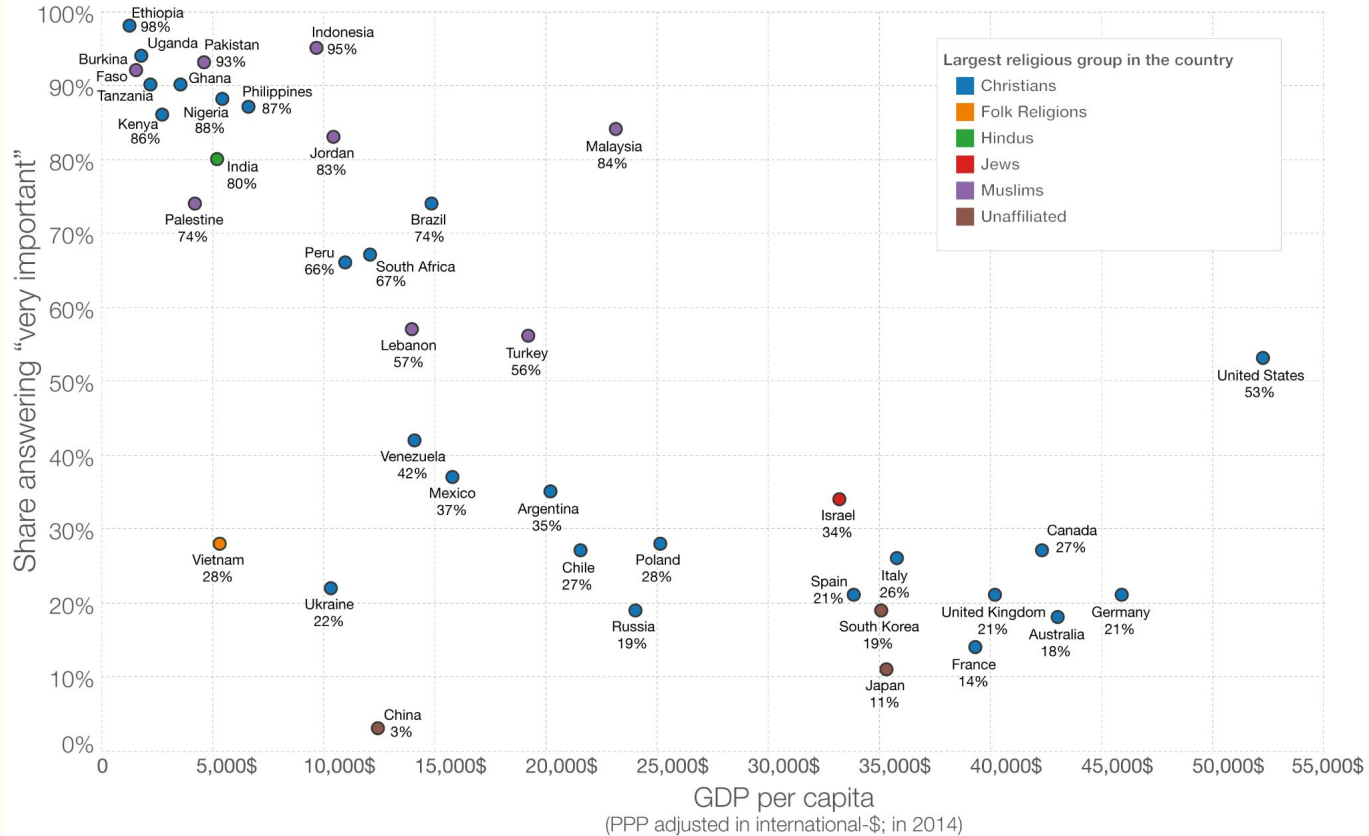
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Importance of Religion vs level of GDP per capita



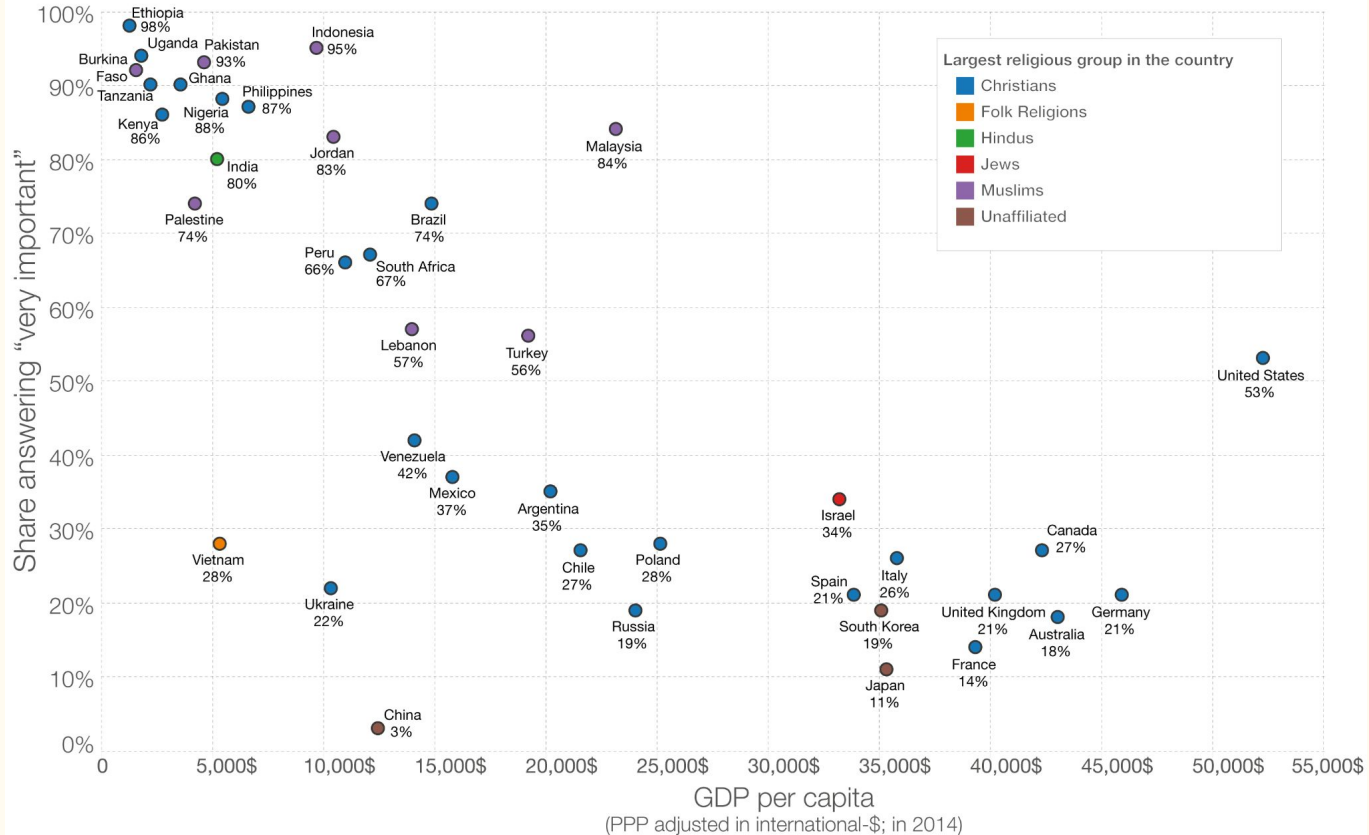
Importance of Religion vs level of GDP per capita



Importance of Religion vs level of GDP per capita

The question that was asked was "How important is religion in your life?" And the possible answers were "very important", "somewhat important", "not too important" and "not at all important". Shown is the share that answered "very important".

The color of each country represents the largest religion in the county. The percentage value is the share answering very important.



Data source: Penn World Table for GDP per capita; Pew Global Attitudes Survey for importance of religion measure; Pew for majority religion.

The interactive data visualization is available at [OurWorldinData.org](https://ourworldindata.org). There you find the raw data and more visualizations on this topic.

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Finding Relationships Between Numerical Variables

Examples:

- Is there a relationship between a student's grade on a midterm exam and their grade on a final exam?
- Is there a relationship between poverty rate in a state and high school graduate rate in that state?

Finding Relationships Between Numerical Variables

What do we want to be able to do?

- Describe how two things are related
 - Visually
 - Qualitatively
 - Quantitatively
- Say whether the relationship is physically and statistically meaningful
- Use the relationship to make predictions

Linear Equations

We'll be looking at **linear equations** in the form

$$y = a + bx,$$

where a and b are constants (numbers).

Some linear equations:

- $y = 3 + 4x$
- $y = 0.01 - 1200x$
- $y = -5x$
- $y = 6x - 2$

Example

Juanita is opening a lemonade stand. She spends \$12 on supplies and then sells lemonade for \$1.50 per cup.

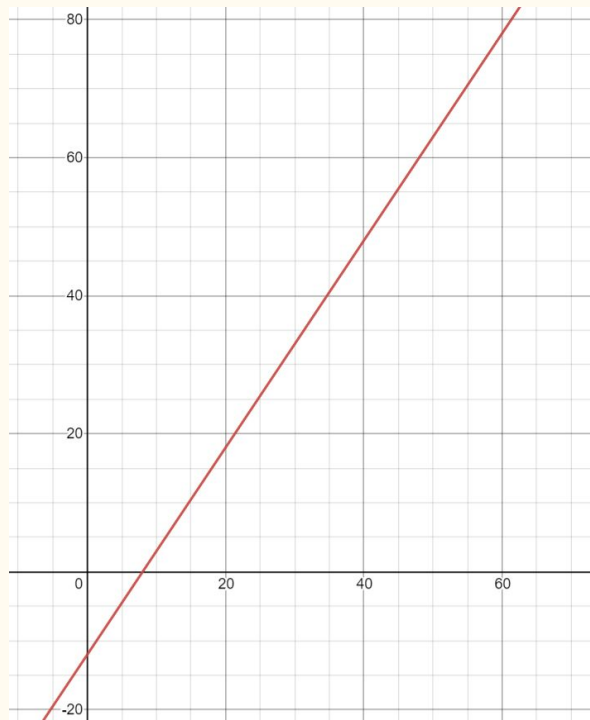
What equation represents her profit p in terms of number of cups sold c ?

Example

Juanita is opening a lemonade stand. She spends \$12 on supplies and then sells lemonade for \$1.50 per cup.

Profit is given by: $p = 1.5c - 12$, where:

- The profit is p .
- The number of cups is c .
- -\$12, the loss to supplies, is the **y-intercept**.
- \$1.50/cup, the price per cup, is the **slope**.



Parts of a Linear Equation

In a linear equation $y = a + bx$:

- The constant term, a , is the **y-intercept**.
- The coefficient of x is the **slope**.

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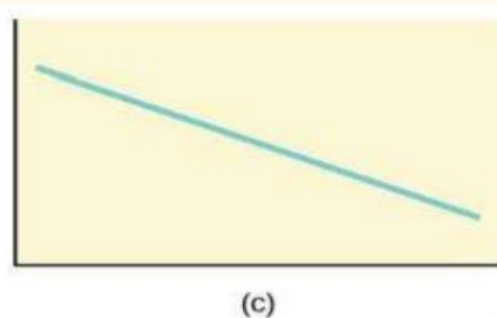
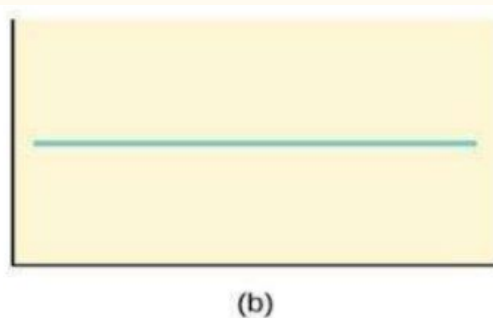
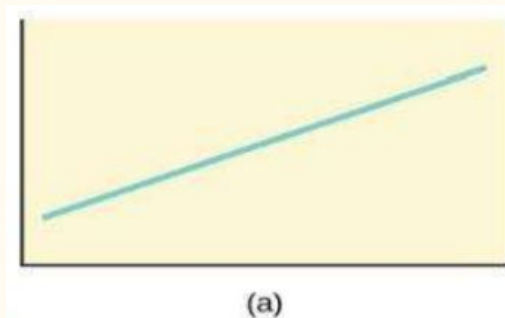
- The constant term, a , is the **y-intercept**.
- The coefficient of x is the **slope**.

Examples:

- In $y = 2700x + 1000$, the y-intercept is 1000, and the slope is 2700.
- In $y = 20 + 0.8x$, the y-intercept is 20, and the slope is 0.8.
- In $y = 5x - 4$, the y-intercept is -4, and the slope is 5.
- In $y = 0.01 - 1200x$, the y-intercept is 0.01, and the slope is -1200.

Interpreting Slope

- Slope tells you how much y changes as x changes by 1 unit.
- **Example:** a slope of 0.8 says that for every increase of x by 1, y will increase by 0.8.
- **Example:** a slope of -2 says for that for every increase of x by 1, y will increase by -2 (so it will decrease by 2!).
- The units of slope are the units of y divided by the units of x .



(a): positive slope

(b): slope = 0

(c): negative slope

Interpreting y-Intercept

- The y-intercept is the y-value where the graph of the line crosses the y-axis.
- It is the y-value when $x = 0$.
- The units of the y-intercept are the units of y .

Example:

For lemonade, $p = 1.5c - 12$

The y-intercept was $-\$12$ because the $\$12$ was an upfront loss, separate from the number of cups of lemonade Juanita sold.

Back to the Example

Juanita is opening a lemonade stand. She spends \$12 on supplies and then sells lemonade for \$1.50 per cup.

Profit is given by: $p = 1.5c - 12$

At the end of the day, Juanita had sold 60 cups of lemonade. What was her profit?

Any initial estimates? (\$20? \$40? \$60? \$80? \$100?)

Back to the Example

At the end of the day, Juanita had sold 60 cups of lemonade. What was her profit?

Profit is given by: $p = 1.5c - 12$

Here, we're told that $c = 60$.

So profit $p = 1.5(60) - 12$

$$p = 90 - 12$$

So the profit is $p = \$78$.

Back to the Example

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Profit is given by: $p = 1.5c - 12$

At the end of the day, Juanita's profit is \$78. How many cups of lemonade did she sell?

Example

Juanita is opening a lemonade stand. She spends \$12 on supplies and then sells lemonade for \$1.50 per cup.

Profit is given by: $p = 1.5c - 12$

At the end of the day, Juanita's profit is \$78. How many cups of lemonade did she sell?

First, an estimate: 25 cups? 50 cups? 75 cups? 100 cups?

Example

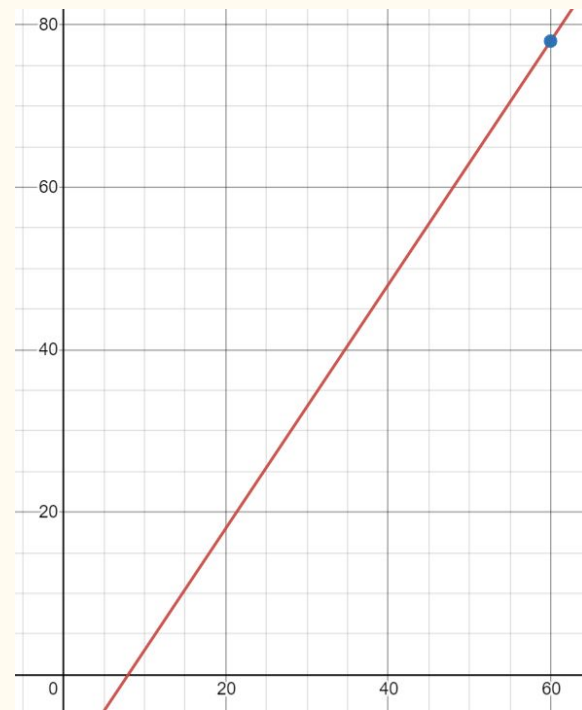
At the end of the day, Juanita's profit is \$78. How many cups of lemonade did she sell?

Profit: $p = 78 = 1.5c - 12$

$$1.5c = 78 + 12$$

So $1.5c = 90$

Then $c = 90/1.5 = 60$ cups of lemonade.



Activity

- Some practice with linear equations
- Some practice with hypothesis testing and paired vs. two-sample data
- Some practice with interpreting histograms