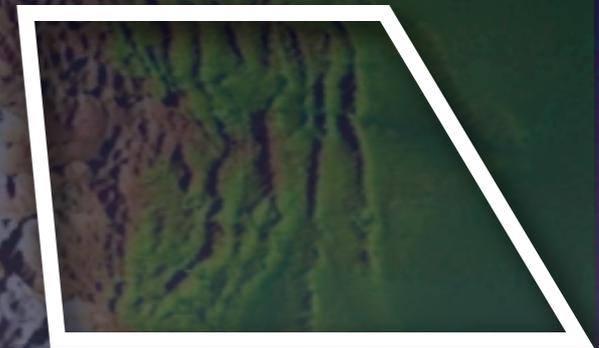


From Decades to Epochs

Intergrating geologic and geodetic
observations of crustal deformation



Jack Loveless
Smith College

Rick Allmendinger
Cornell University

Comparing Geodetic & Geologic Rates

- Strain analysis
 - Nothing more than the gradients in the displacement/velocity fields
 - Good for regional analysis, not so good for individual faults
- Elastic block modeling
 - Based on active fault maps
 - Provides a prediction of fault slip rates
 - Faults can only terminate against other faults

Calculating Strain from a Displacement Field

displacement

$$u_i = t_i + \frac{\partial u_i}{\partial X_j} X_j = t_i + e_{ij} X_j$$

position

displacement
gradient tensor

In 1D, e_{ij} is just the extension:

$$e = \frac{\Delta u}{\Delta X} = \frac{l_{final} - l_{initial}}{l_{initial}}$$

Strain From Displacement Vectors

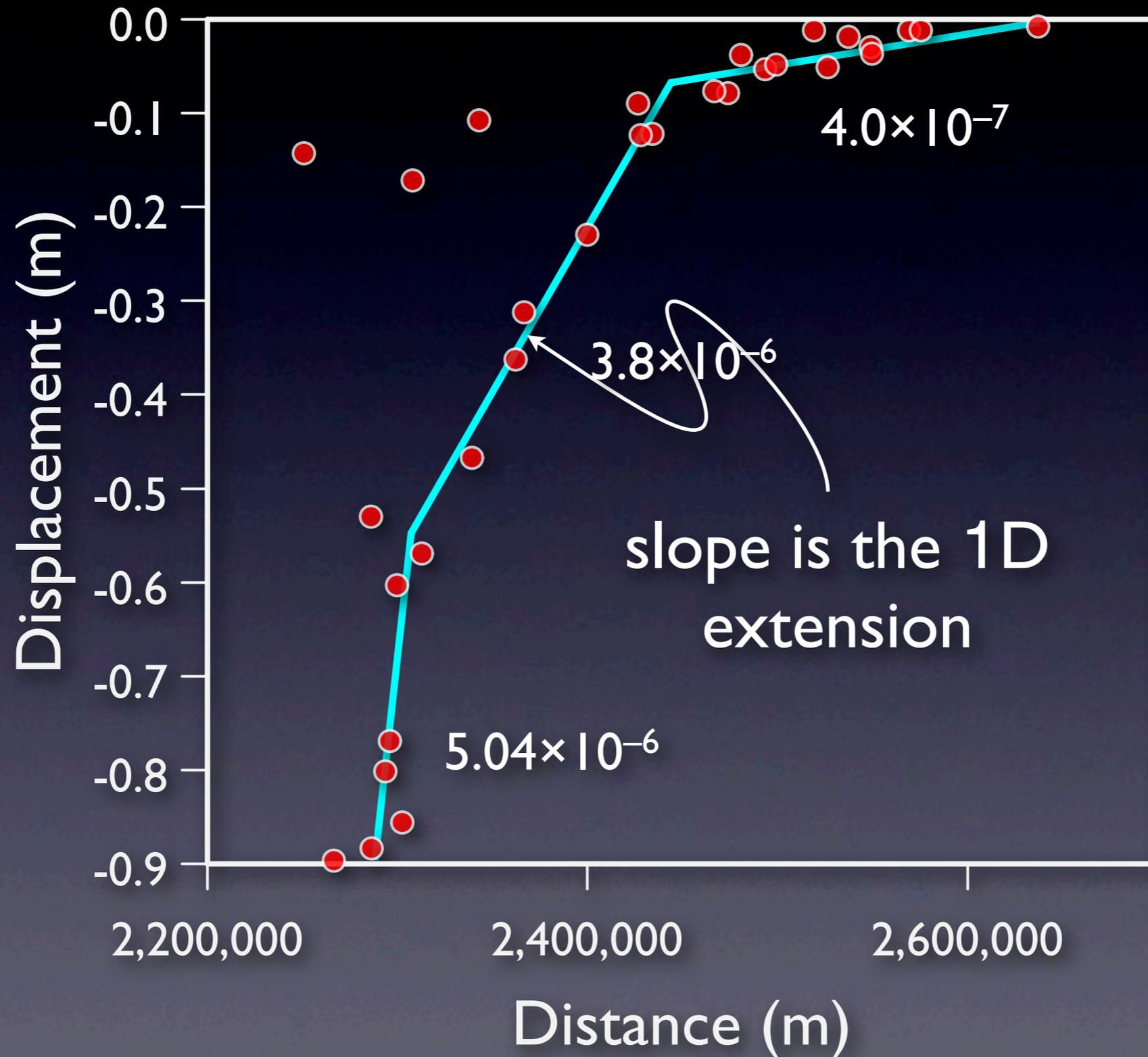


1D Transect

rotate coordinate system so it parallels the mean vector

vectors from Klotz
et al (1999)

Strain From Displacement Vectors



Strain From Displacement Vectors



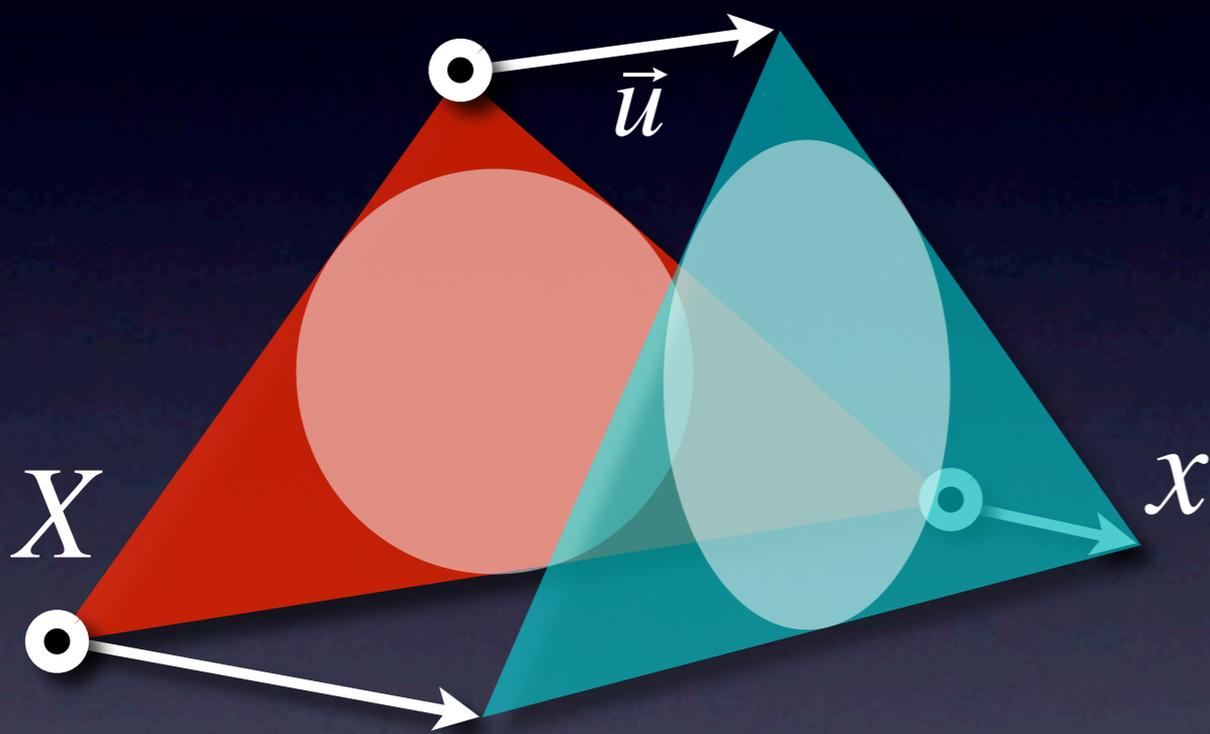
these secondary gradients often explain why major structures are not \perp to displacement vectors

but, there are gradients \perp to the transect, too!

The Inverse Problem

$$u_i = t_i + e_{ij} X_j$$

knowns



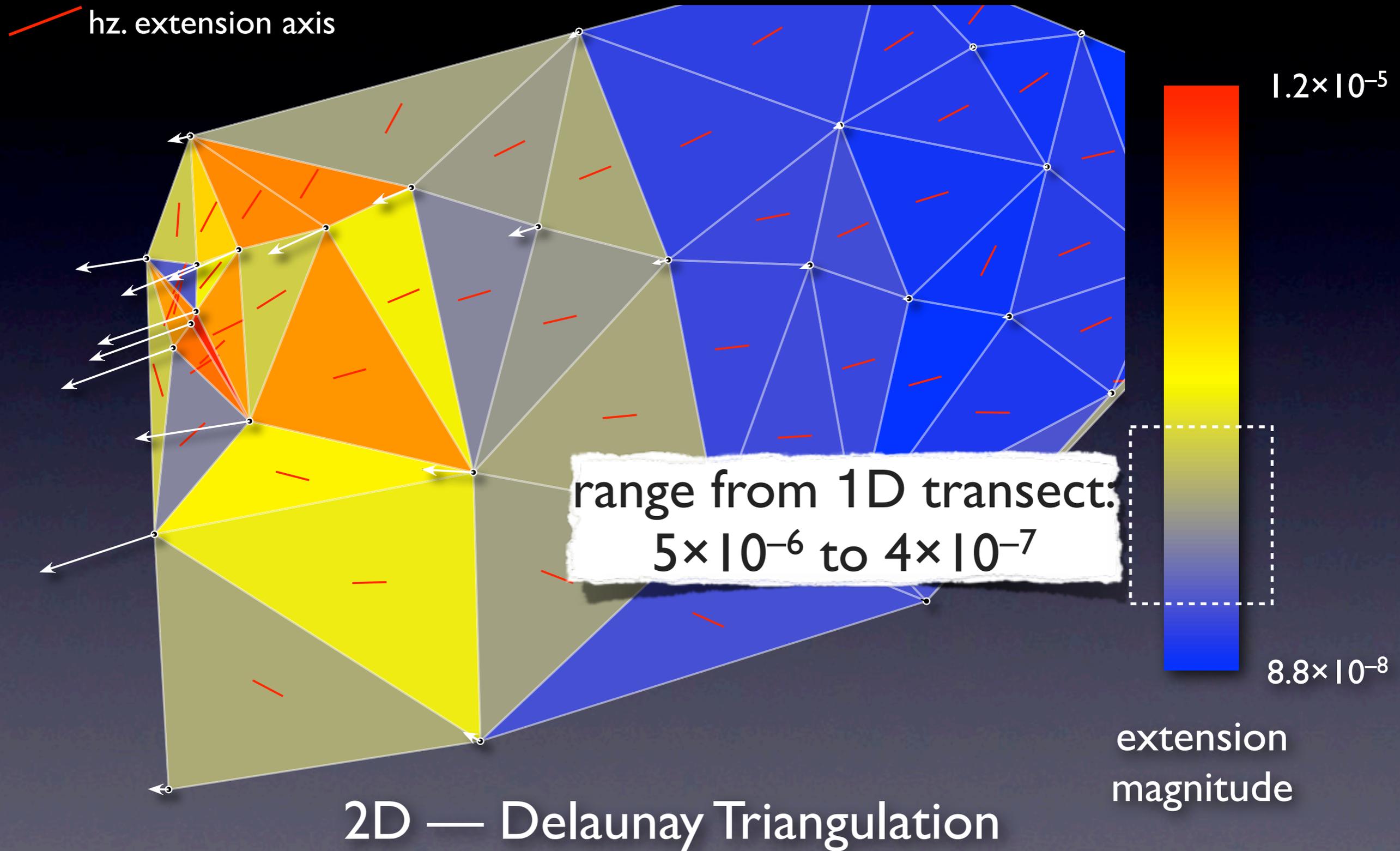
solve for the 6 unknowns

each station & vector gives two equations

$n \geq 3$ (in 2D)

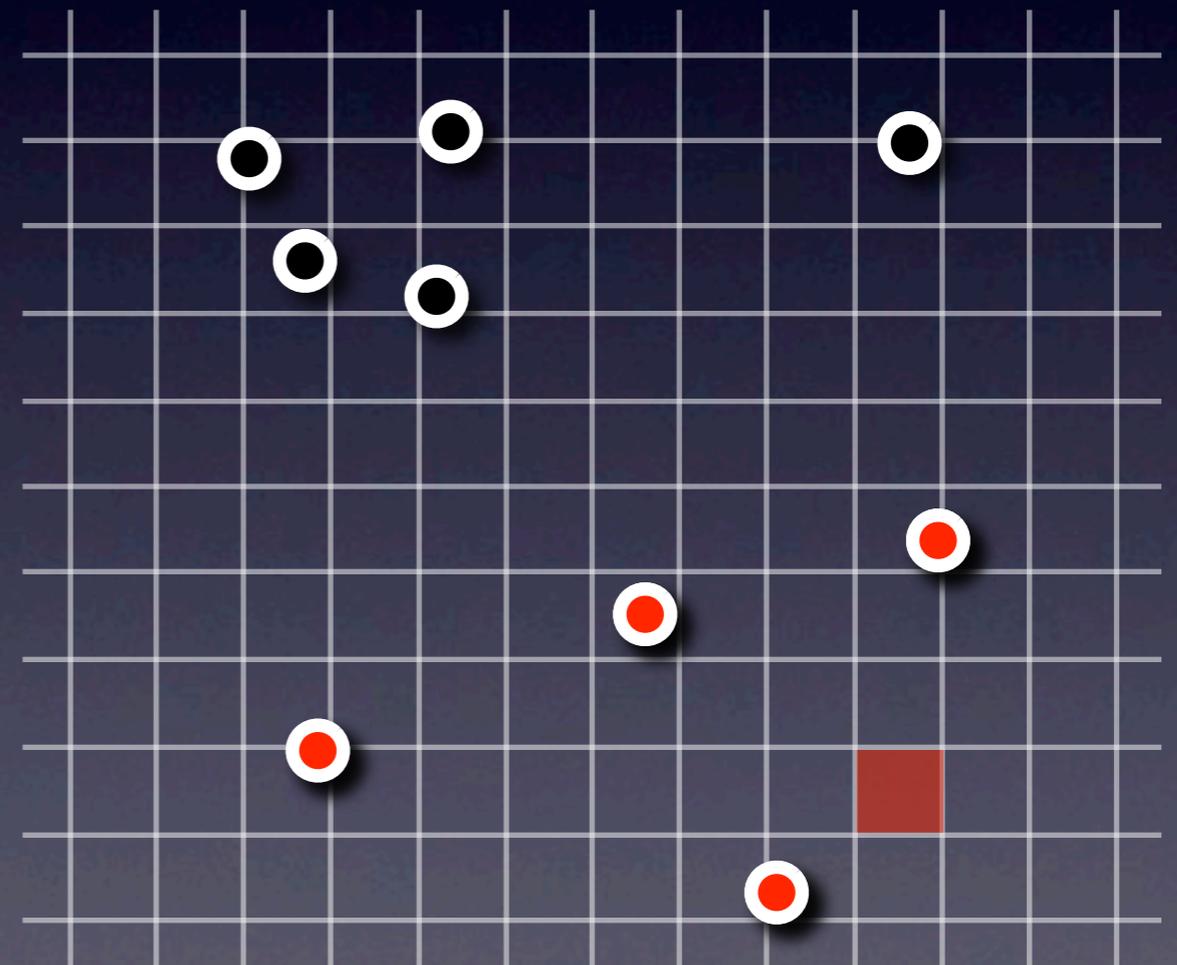
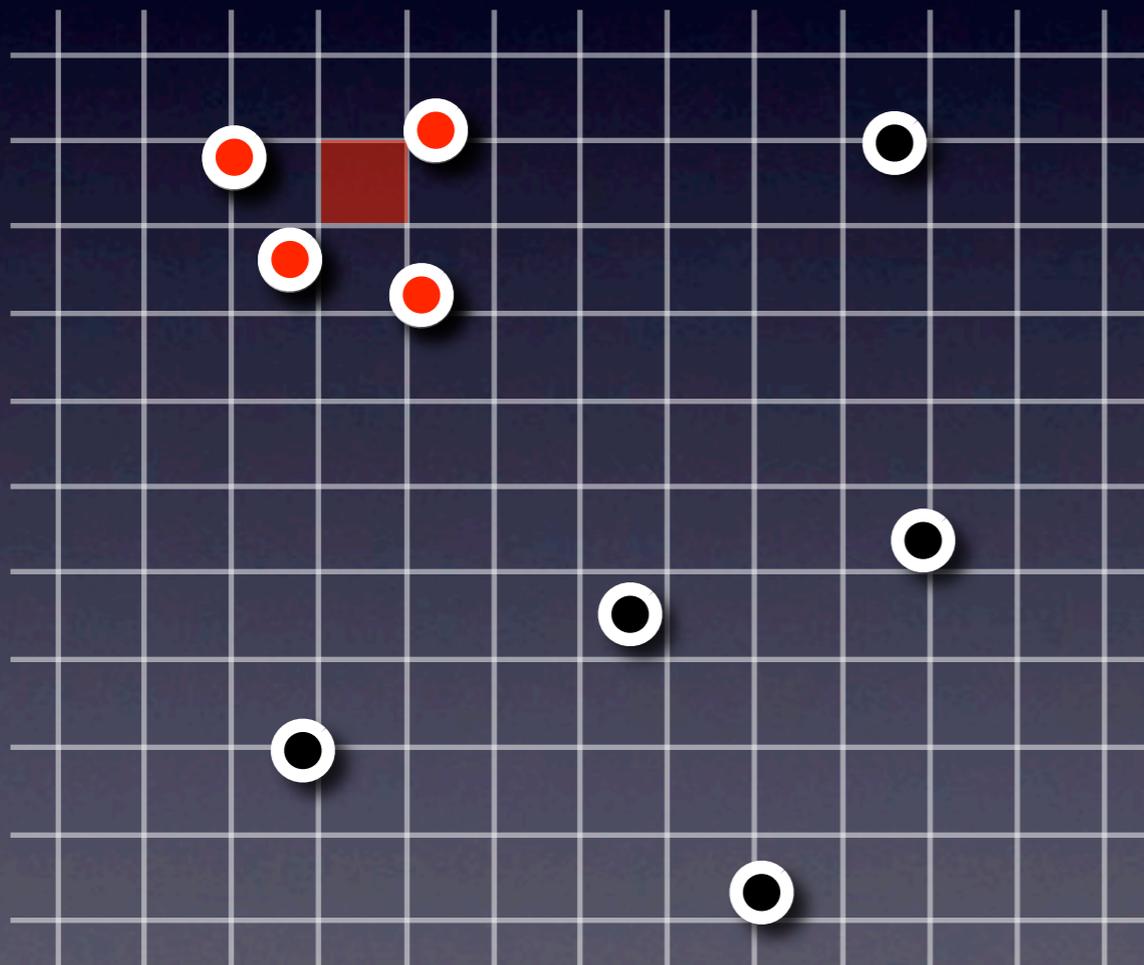
$$\begin{bmatrix} 1u_1 \\ 1u_2 \\ 2u_1 \\ 2u_2 \\ \dots \\ \dots \\ nu_1 \\ nu_2 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 1X_1 & 1X_2 & 0 & 0 \\ 0 & 1 & 0 & 0 & 1X_1 & 1X_2 \\ 1 & 0 & 2X_1 & 2X_2 & 0 & 0 \\ 0 & 1 & 0 & 0 & 2X_1 & 2X_2 \\ \dots & \dots & \dots & \dots & \dots & \dots \\ \dots & \dots & \dots & \dots & \dots & \dots \\ 1 & 0 & nX_1 & nX_2 & 0 & 0 \\ 0 & 1 & 0 & 0 & nX_1 & nX_2 \end{bmatrix} \begin{bmatrix} t_1 \\ t_2 \\ e_{11} \\ e_{12} \\ e_{21} \\ e_{22} \end{bmatrix}$$

Strain From Displacement Vectors



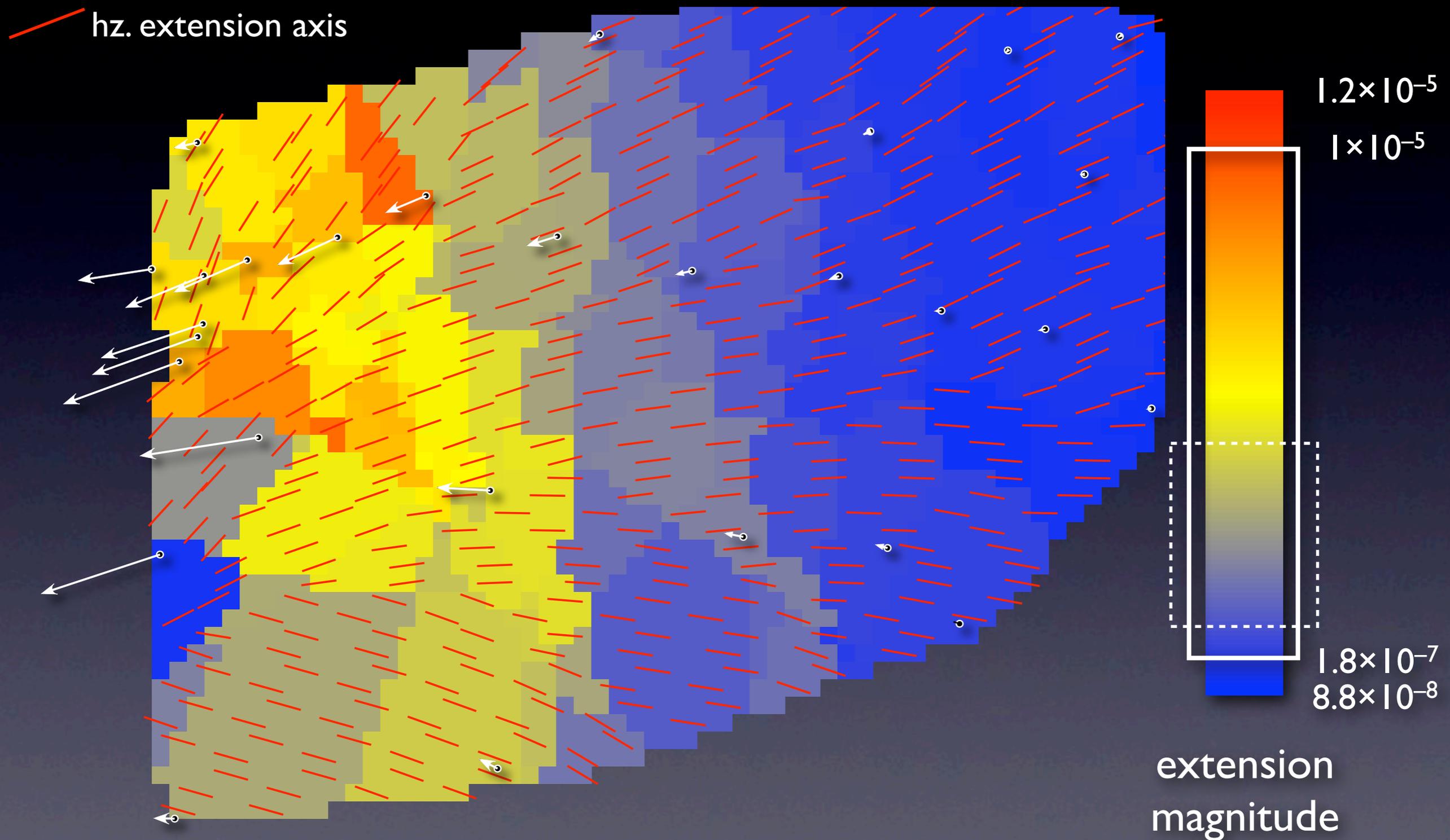
Calculate a regularly-spaced velocity gradient field from irregularly spaced data

Strategy I: Nearest Neighbors (e.g., $n = 4$)



each grid node has different spatial significance!

Strain From Displacement Vectors

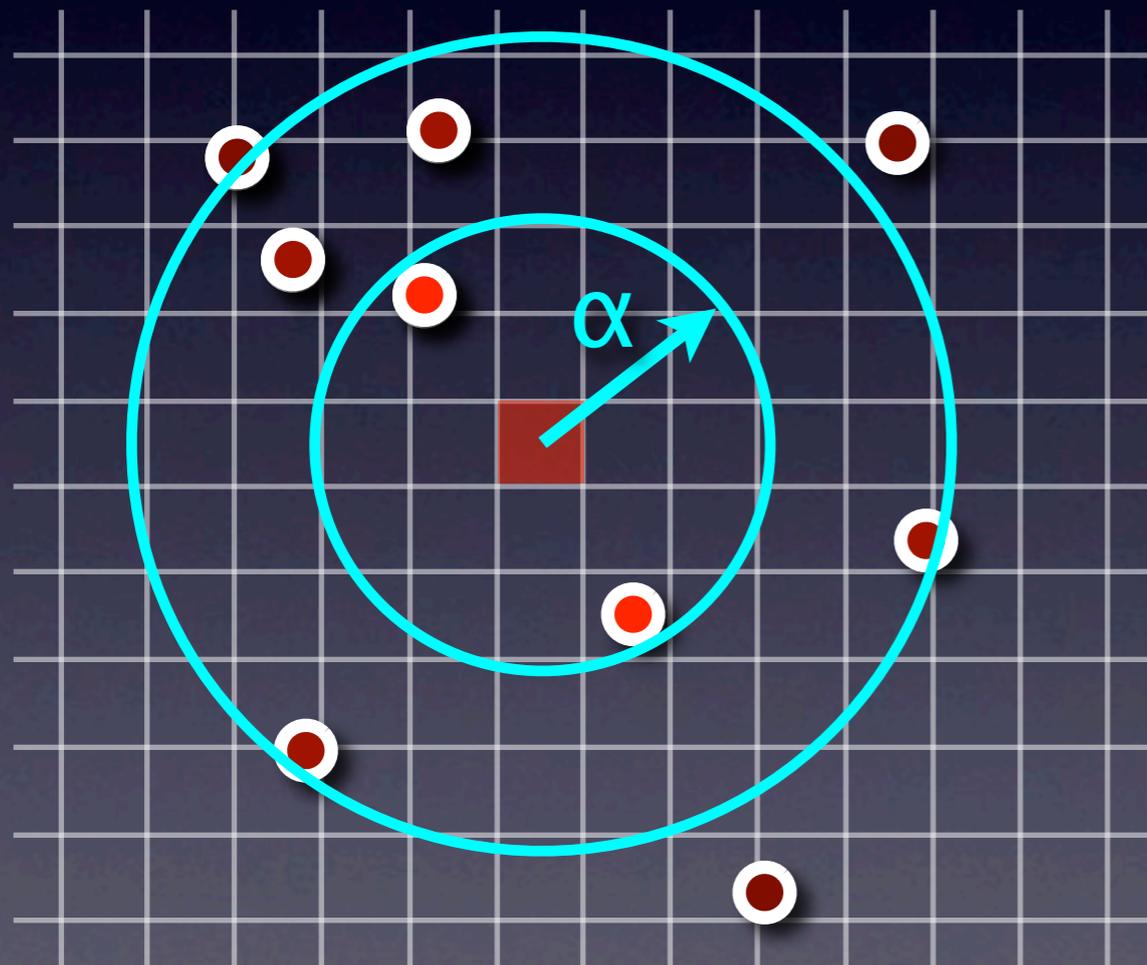


2D — Nearest Neighbor Least Squares

$n = 6$

Calculate a regularly-spaced velocity gradient field from irregularly spaced data

Strategy 2: Distance Weighted (Shen et al., 1996)



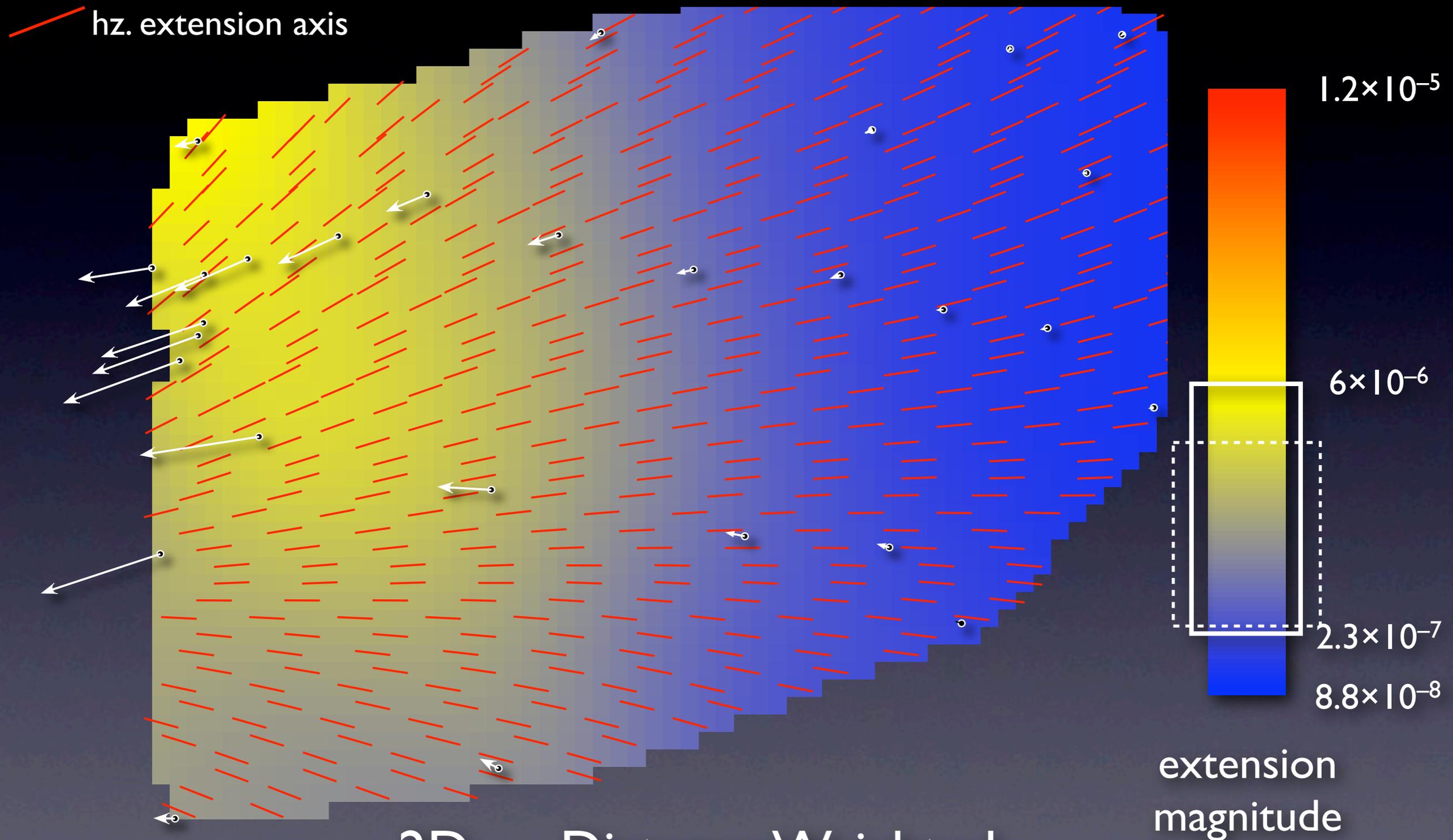
spatial variation is smoothed out

- all stations used in calculation for each grid node
- contribution of each station weighted by distance from node
- use a weighted least squares solution (Menke, 1984):

$$\mathbf{m} = \left[\mathbf{G}^T \mathbf{W} \mathbf{G} \right]^{-1} \mathbf{G}^T \mathbf{W} \mathbf{d}$$

$$\mathbf{W} = \exp\left(\frac{-dist^2}{2\alpha^2}\right)$$

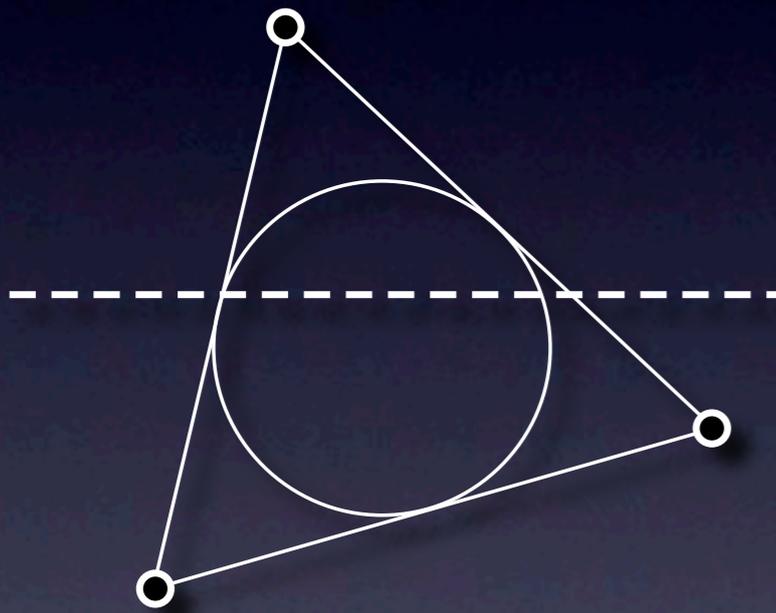
Strain From Displacement Vectors



2D — Distance Weighted

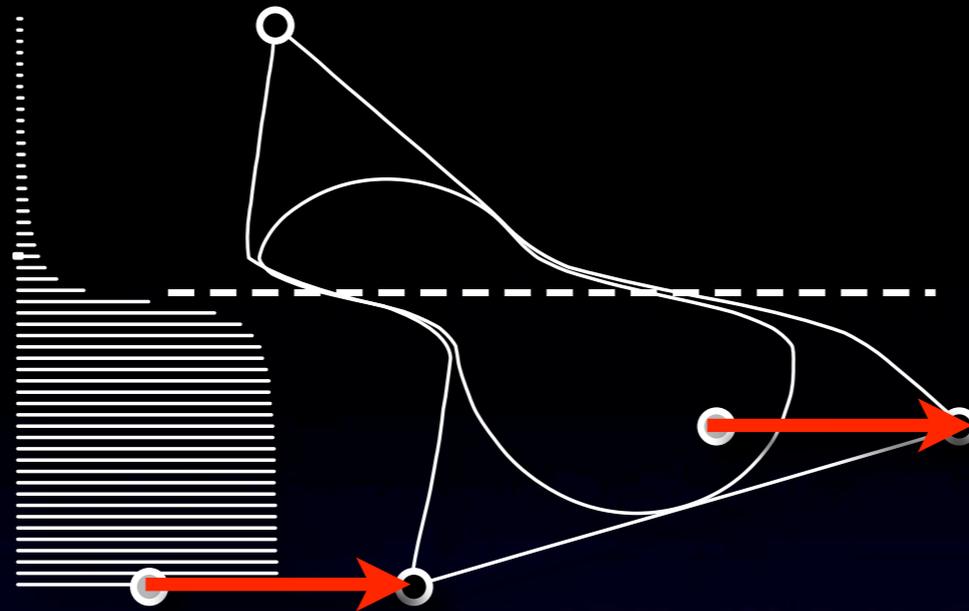
$$\mathbf{m} = \left[\mathbf{G}^T \mathbf{W} \mathbf{G} \right]^{-1} \mathbf{G}^T \mathbf{W} \mathbf{d} \quad \text{where} \quad \mathbf{W} = \exp\left(\frac{-dist^2}{2\alpha^2}\right)$$

Strain & Faulting

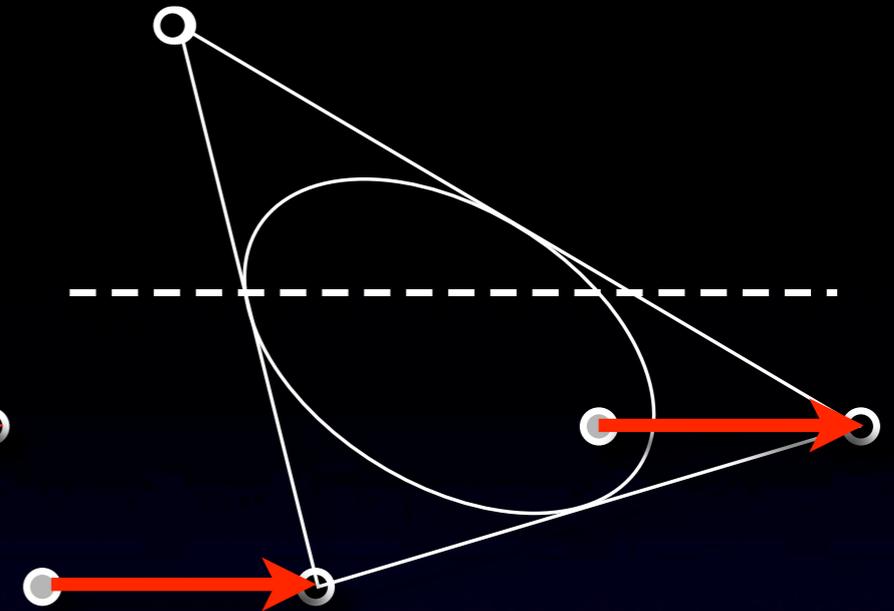


Strain & Faulting

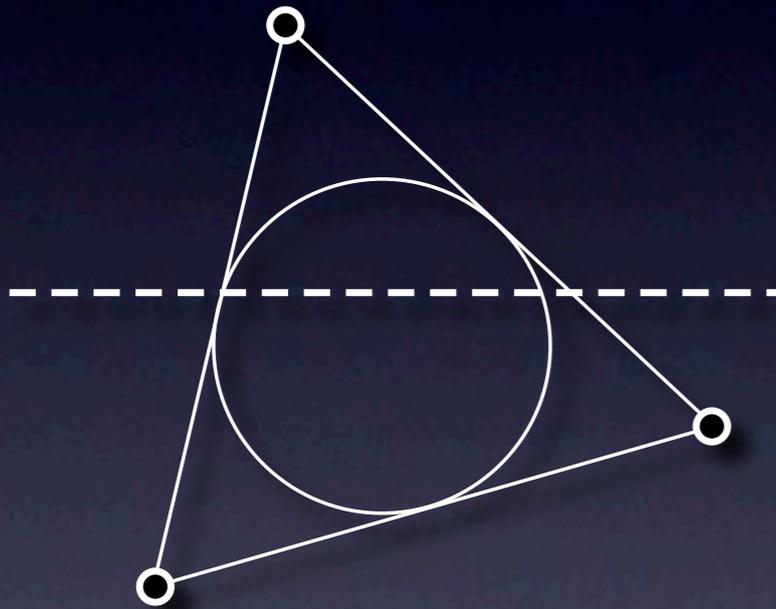
what is really happening



what the GPS network sees

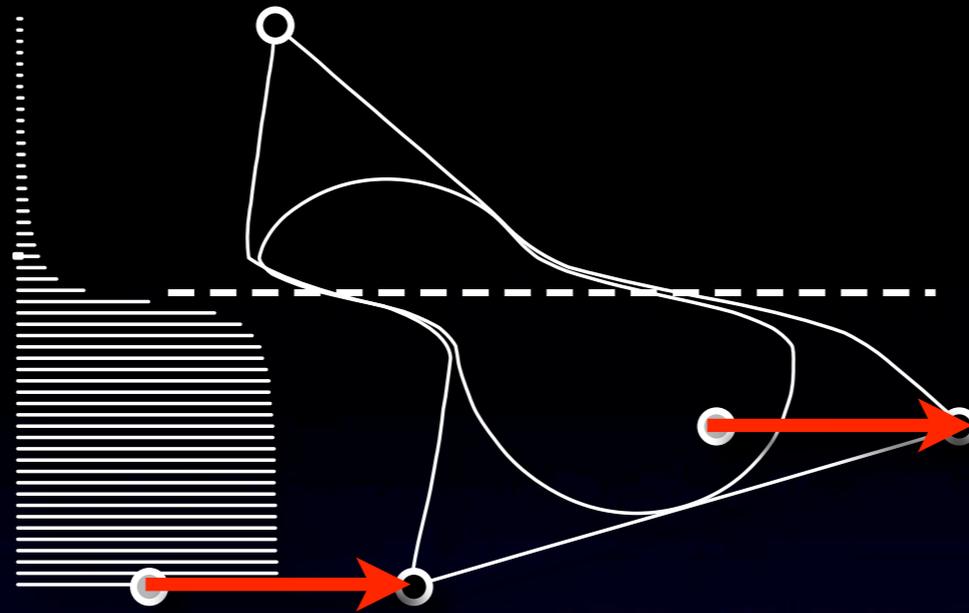


Interseismic

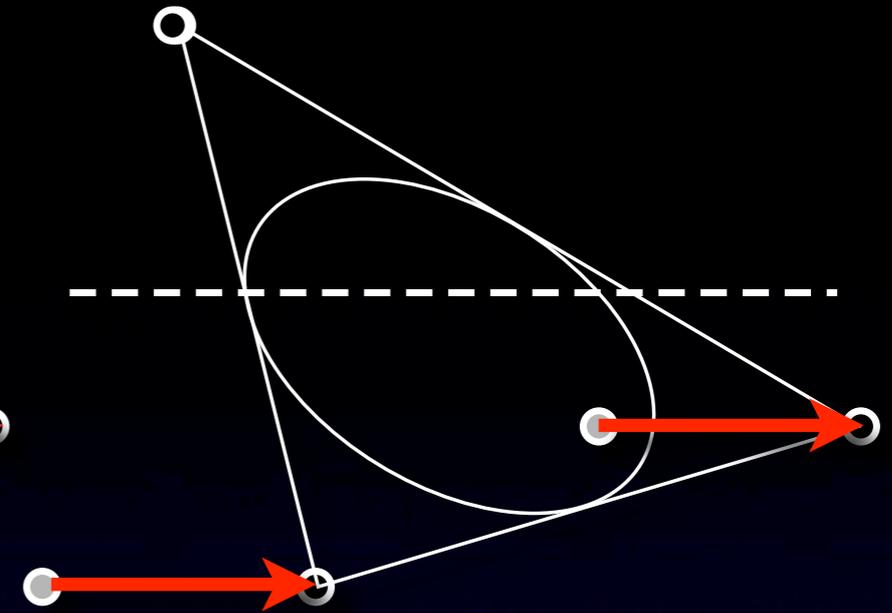


Strain & Faulting

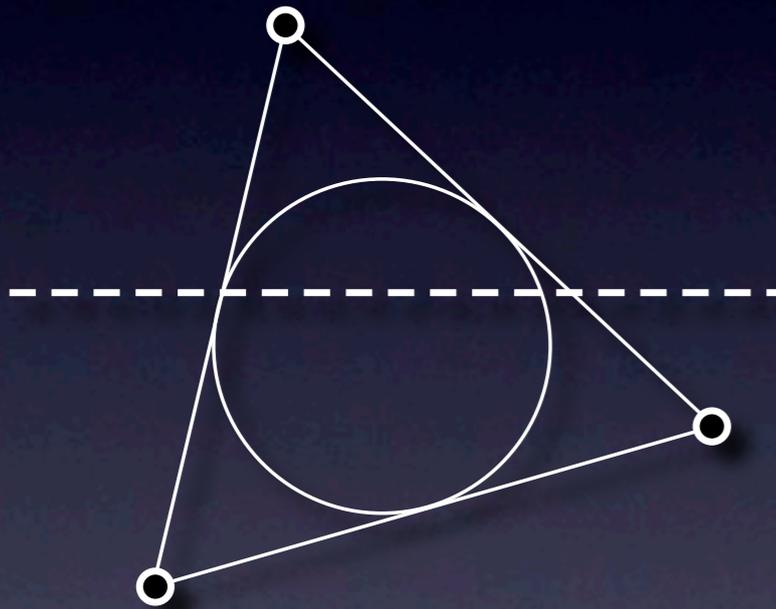
what is really happening



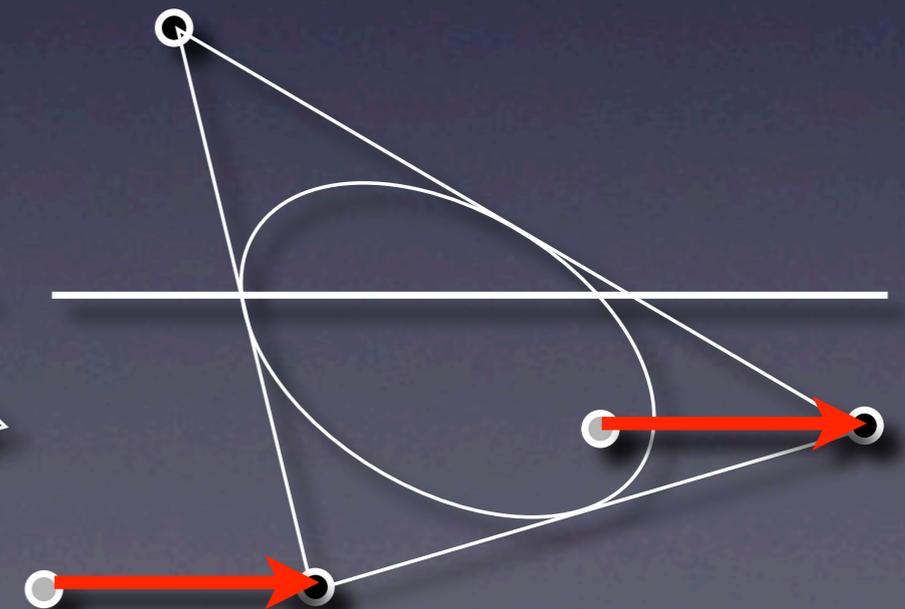
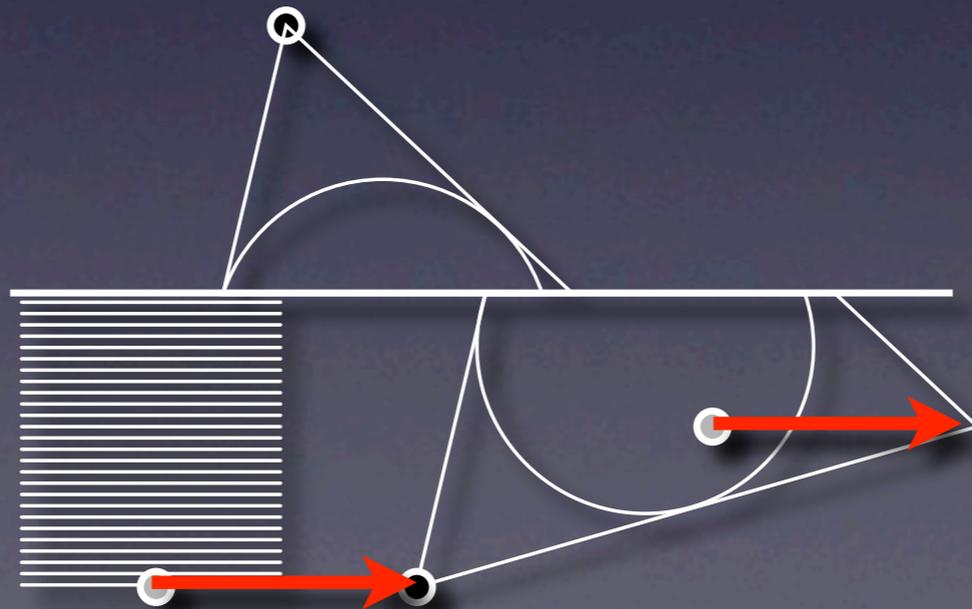
what the GPS network sees



Interseismic

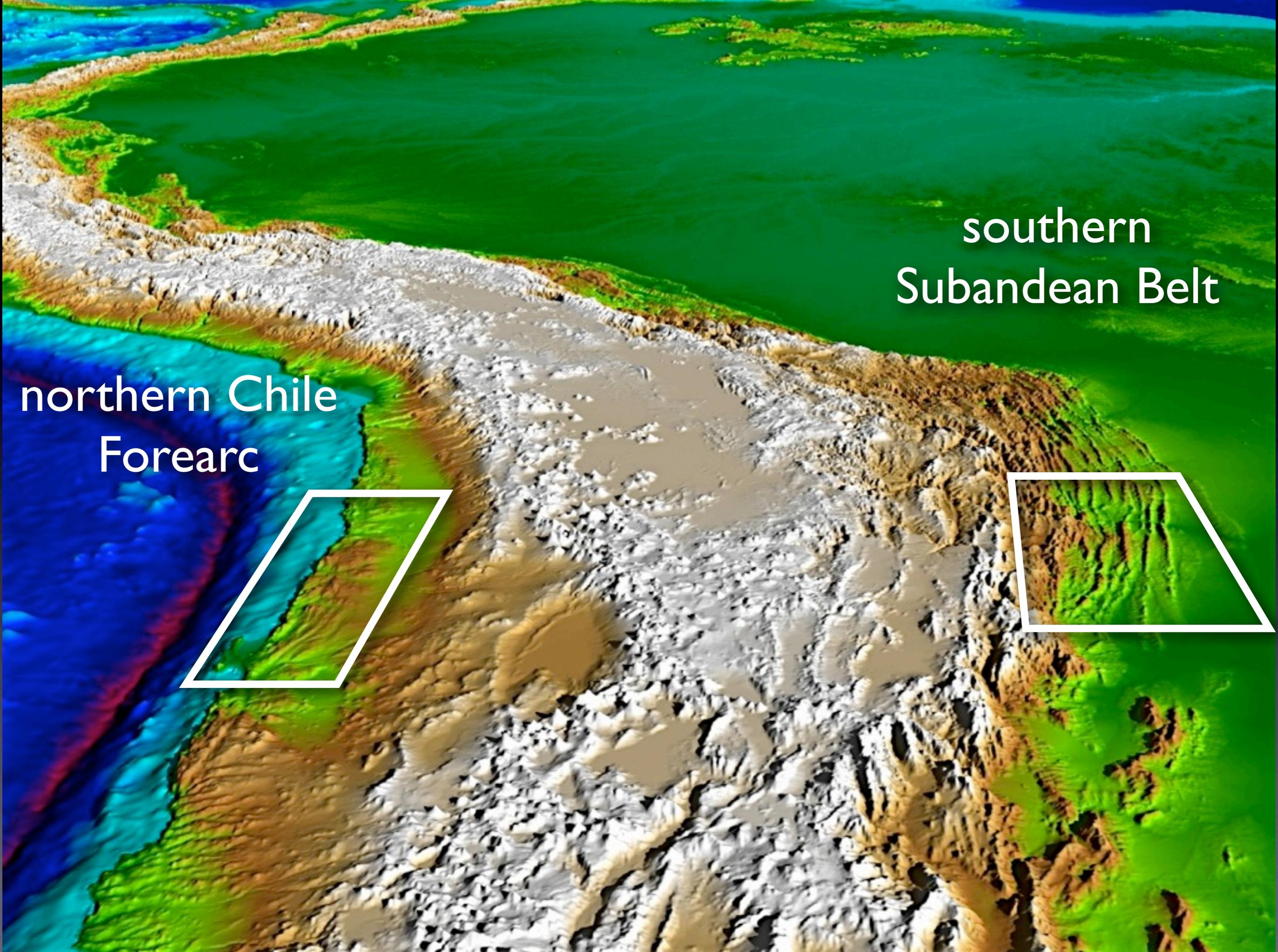


Complete Cycle



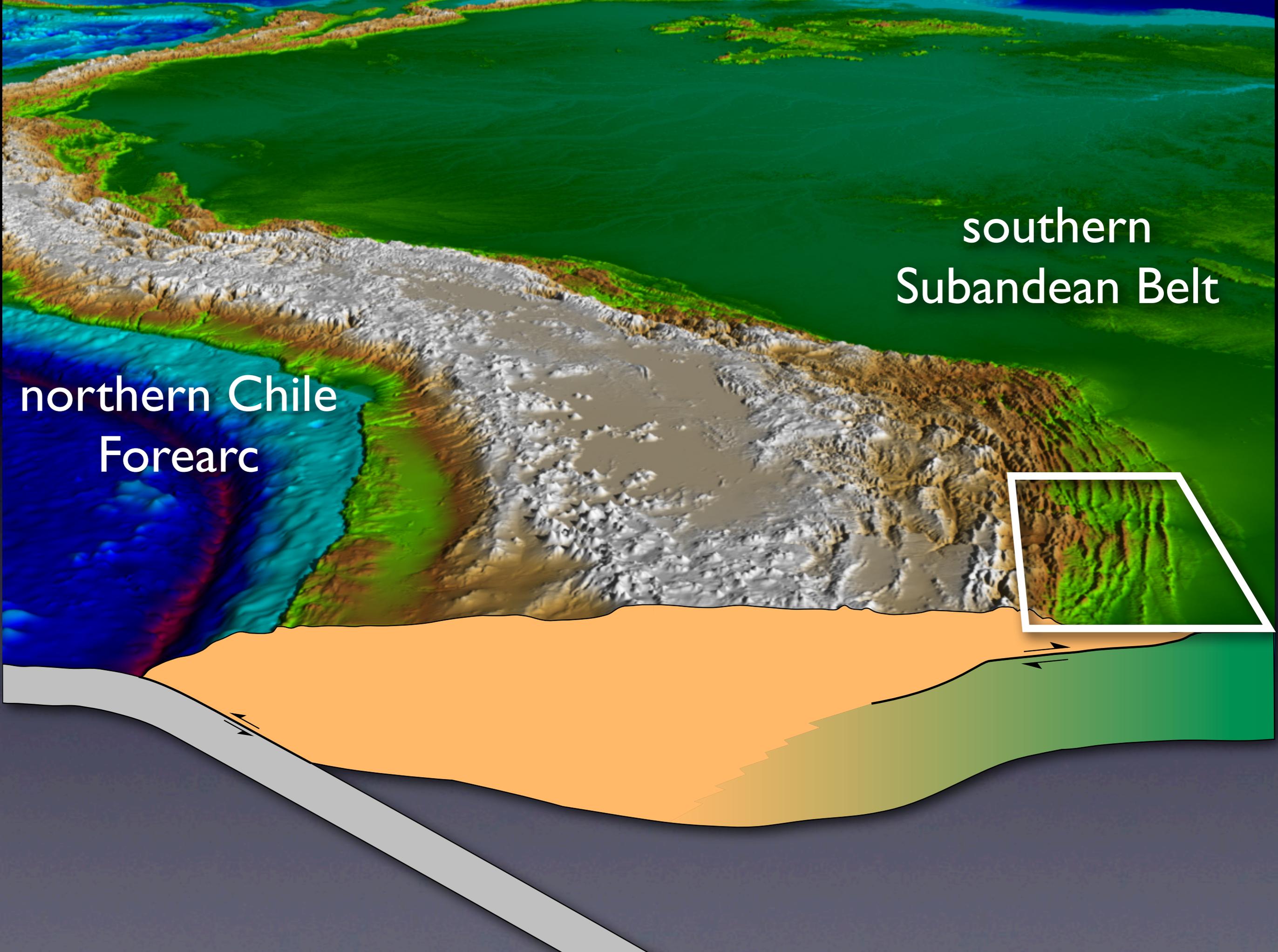
Interseismic and Long Term Strain

- Geodetic strain during the interseismic part of the seismic cycle should match the long term geologic strain (where networks cross major faults)
- Need very dense networks to differentiate between creeping faults and those that are locked interseismically



northern Chile
Forearc

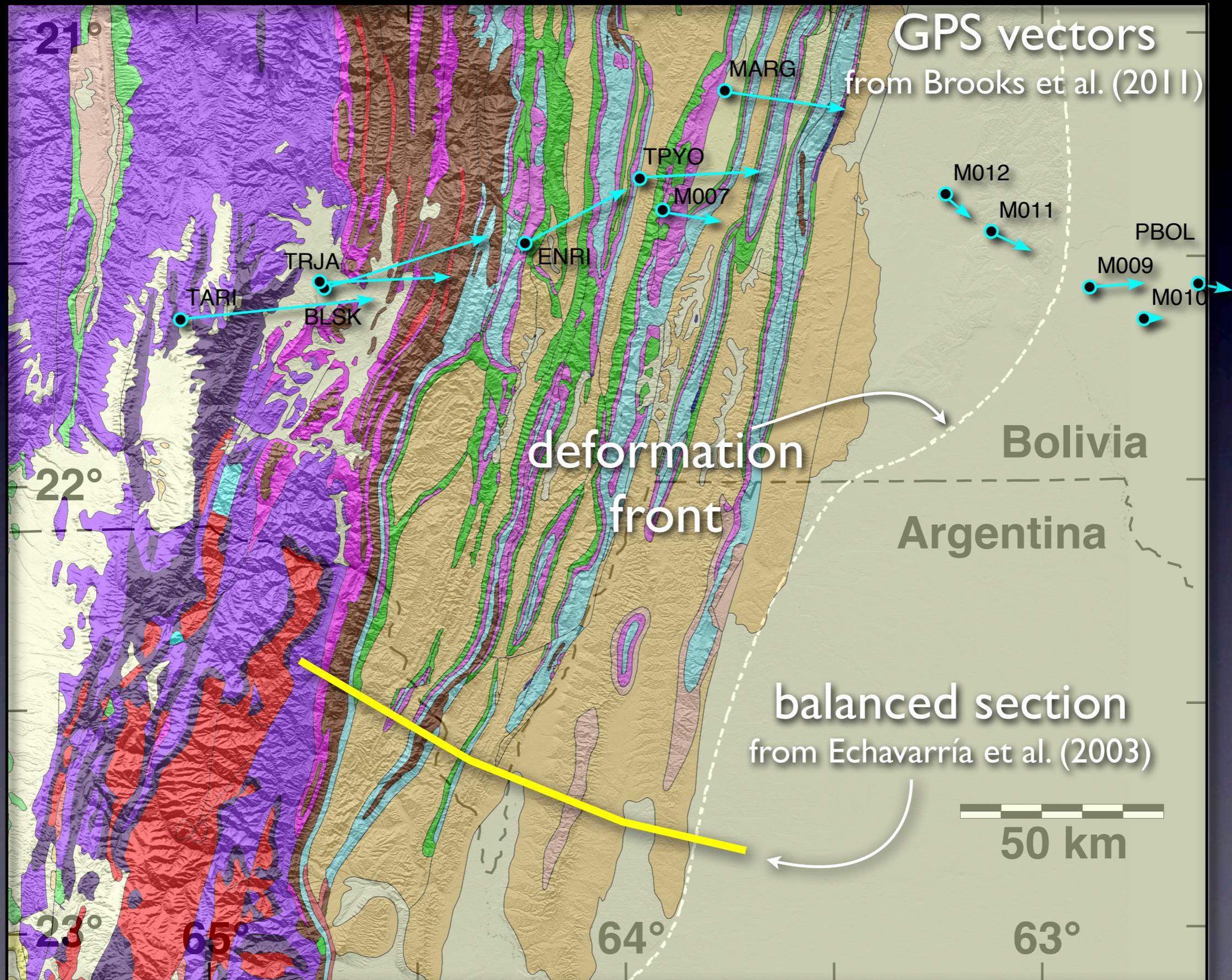
southern
Subandean Belt



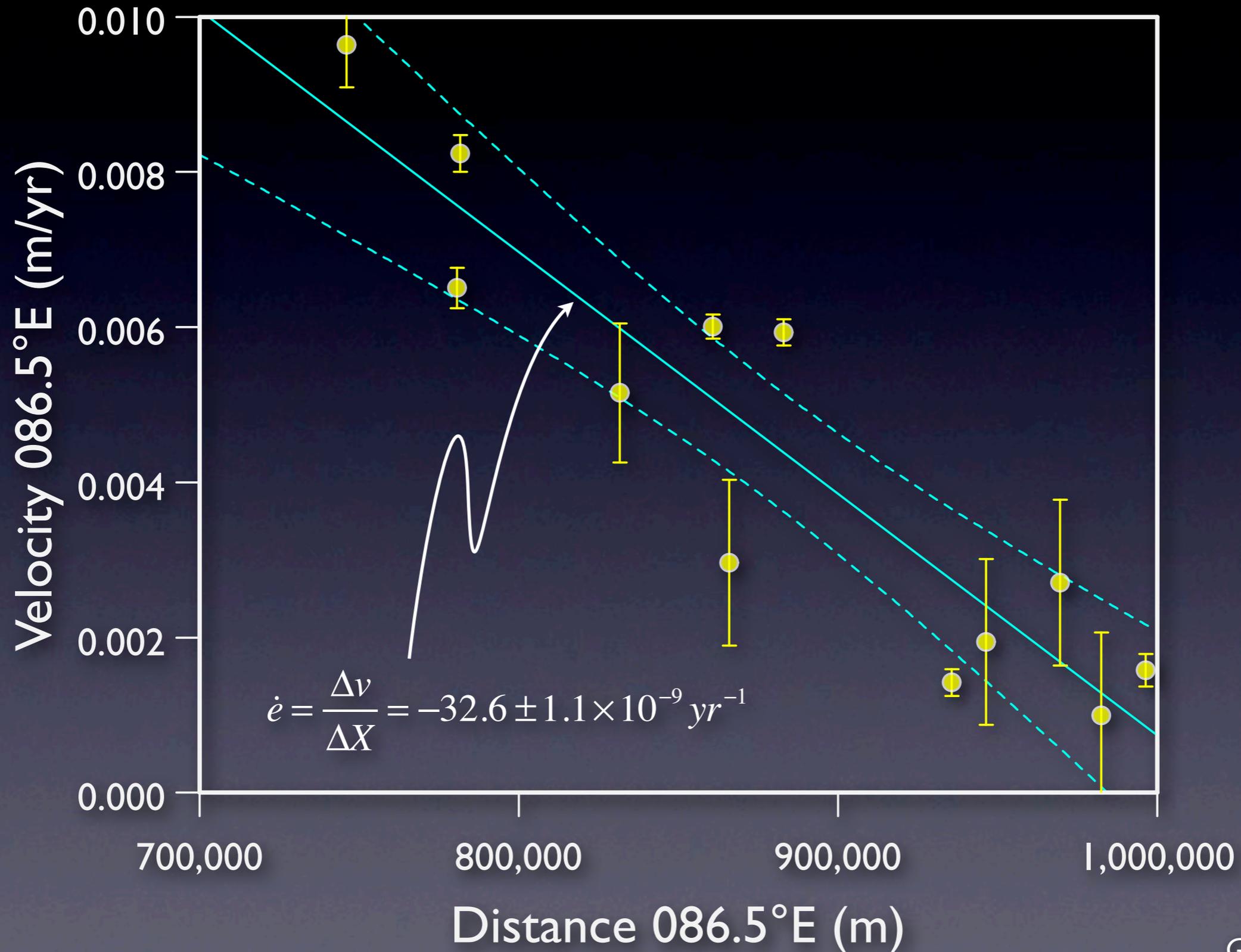
northern Chile
Forearc

southern
Subandean Belt

Southern Subandean Thrust Belt

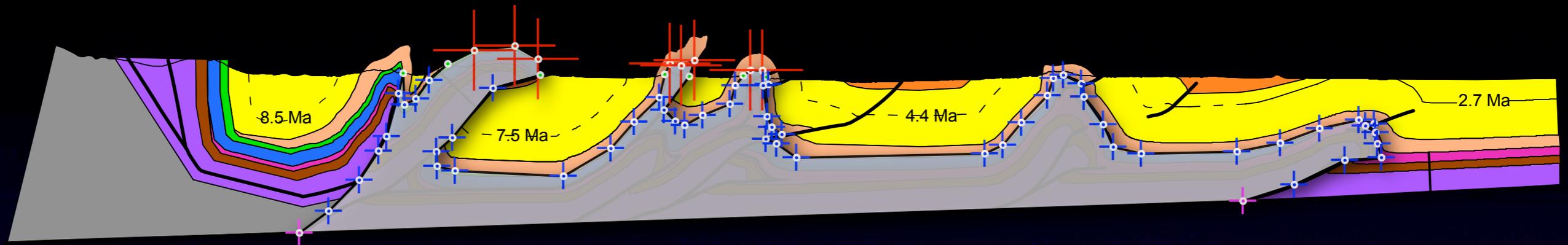


Subandean GPS Interseismic Strain Rate

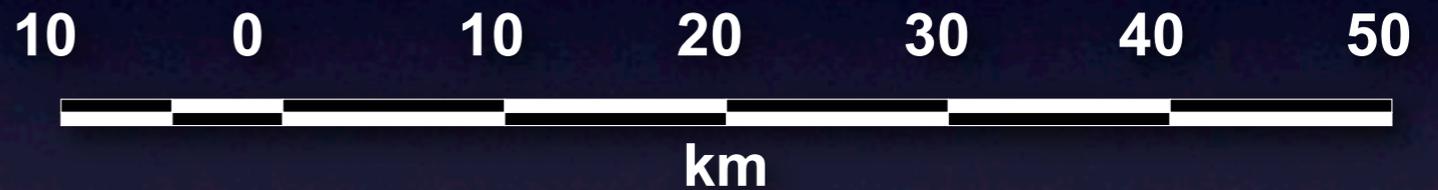


GPS data
from Brooks et al. (2011)

Subandean Balanced Section



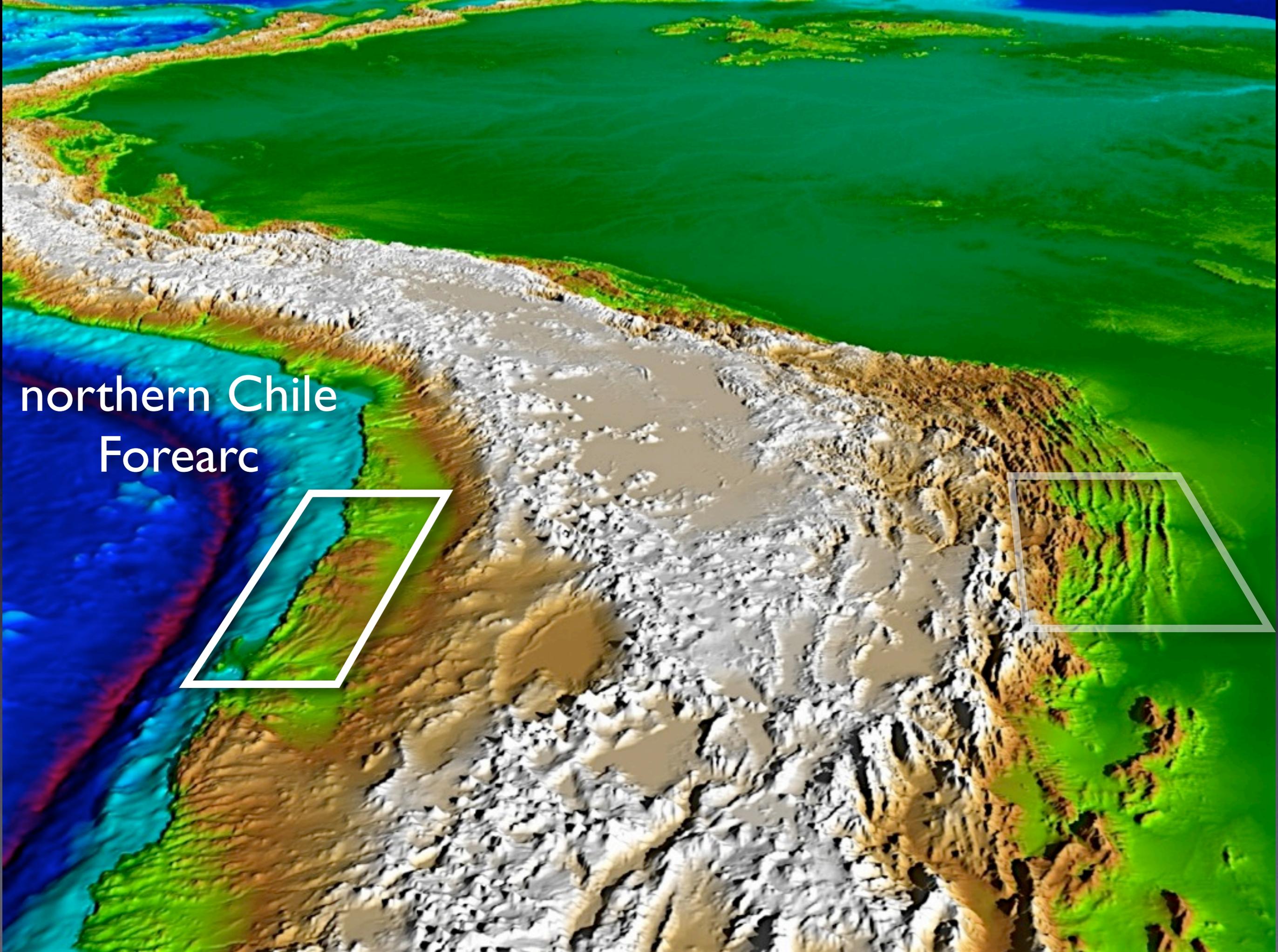
Echavarría et al. (2003)
Judge & Allmendinger (2011)



		Error	
		Gaussian	Maximum
Shortening:	49.58	± 18.71	90.48
Shortening percent:	38.39	± 8.97	43.76

Geology: $-38.4 \pm 9 \times 10^{-9} \text{ yr}^{-1}$ for 10 Ma

GPS: $-32.6 \pm 1.1 \times 10^{-9} \text{ yr}^{-1}$ for 10 yr



northern Chile
Forearc

Interplate Seismicity Since 1900



10°S

20°S

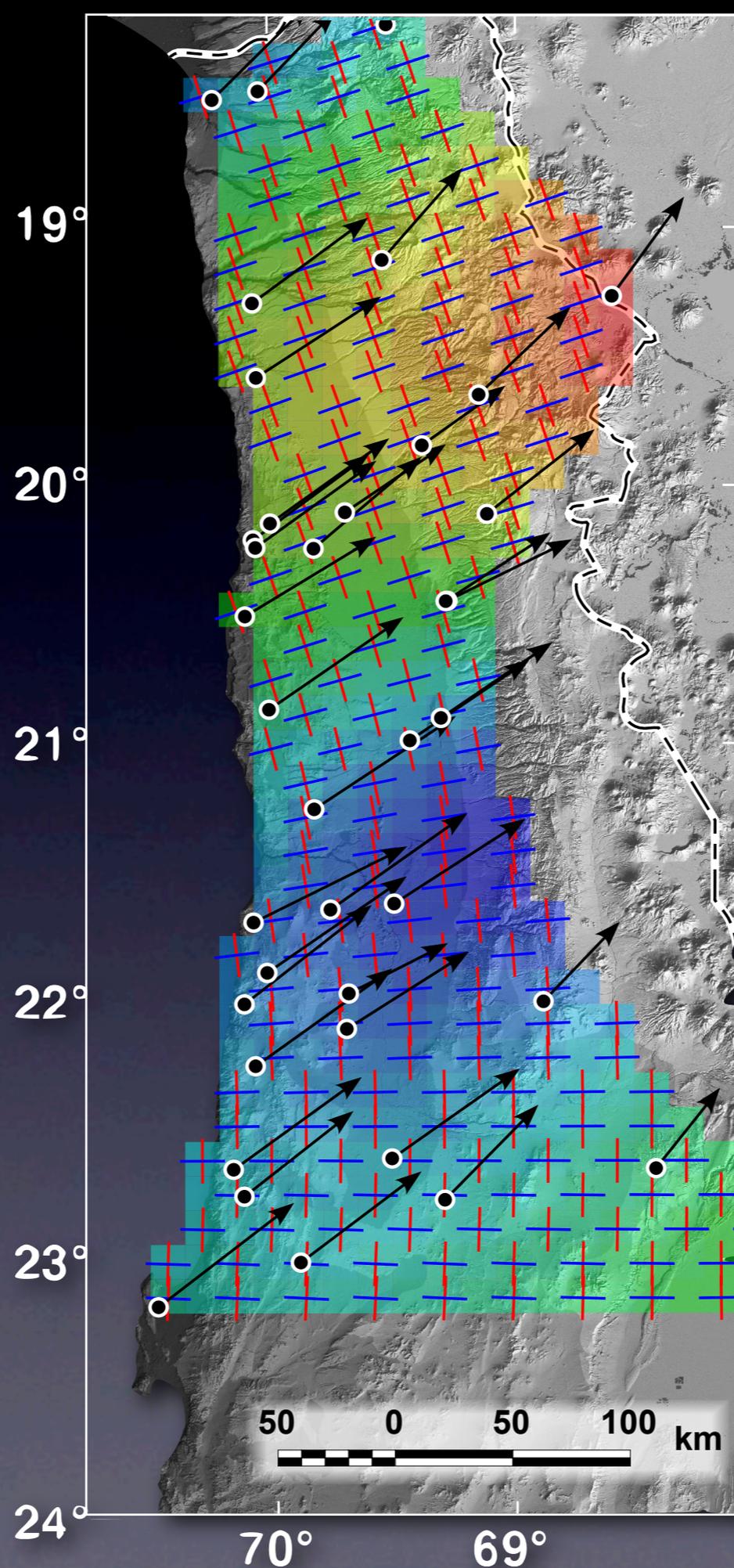
30°S

40°S

Iquique Gap

Northern Chile cGPS

cGPS stations from Caltech, IRD, & IPGP



shortening magnitude

-41.2

-75.1

$\times 10^{-9} \text{ yr}^{-1}$

shortening rate axes

extension rate axes

Coastal Cordillera near Antofagasta

Mejillones
Peninsula

Antofagasta 



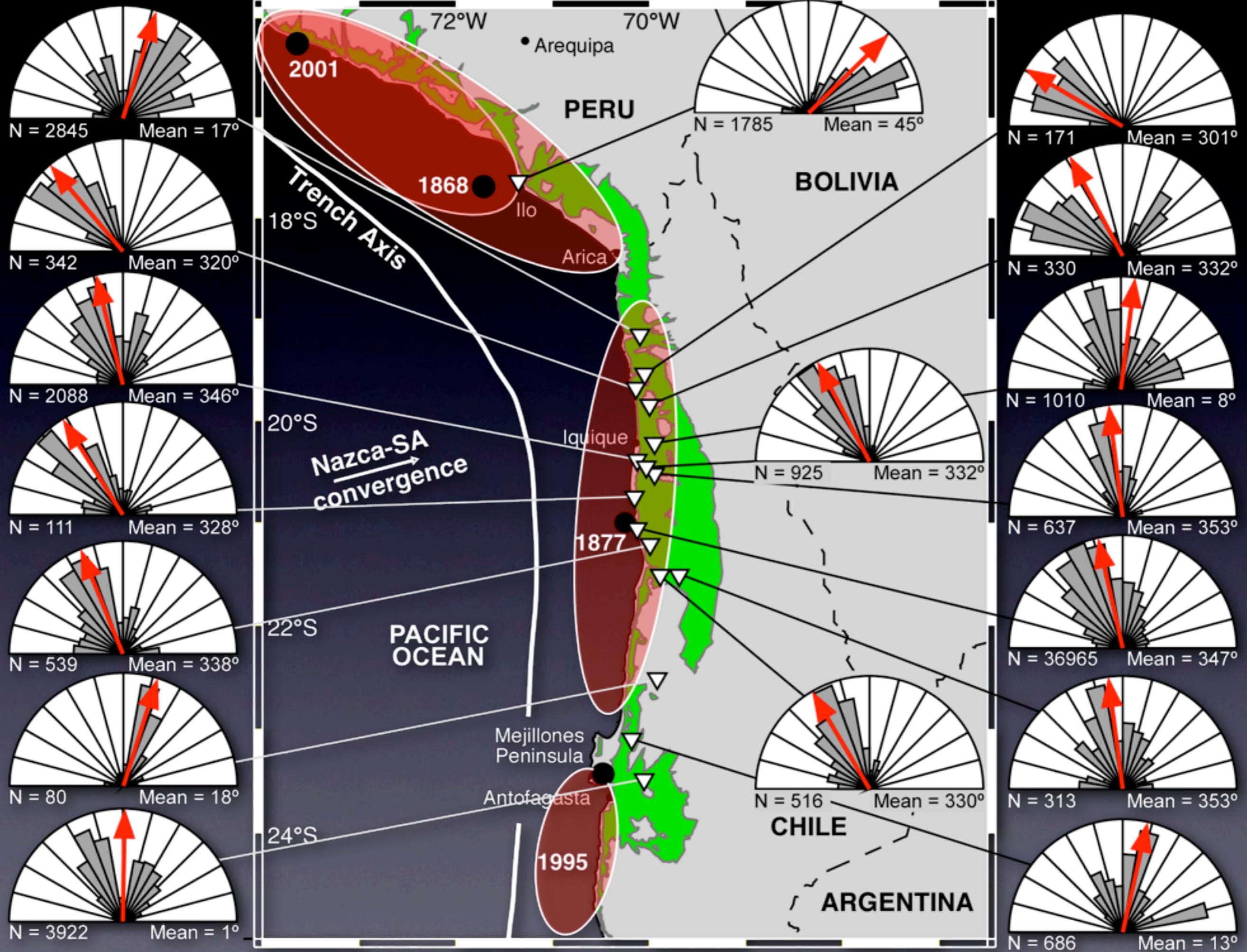
Caleta Herradura—Mejillones Peninsula



Crack Network at Mantos Blanco



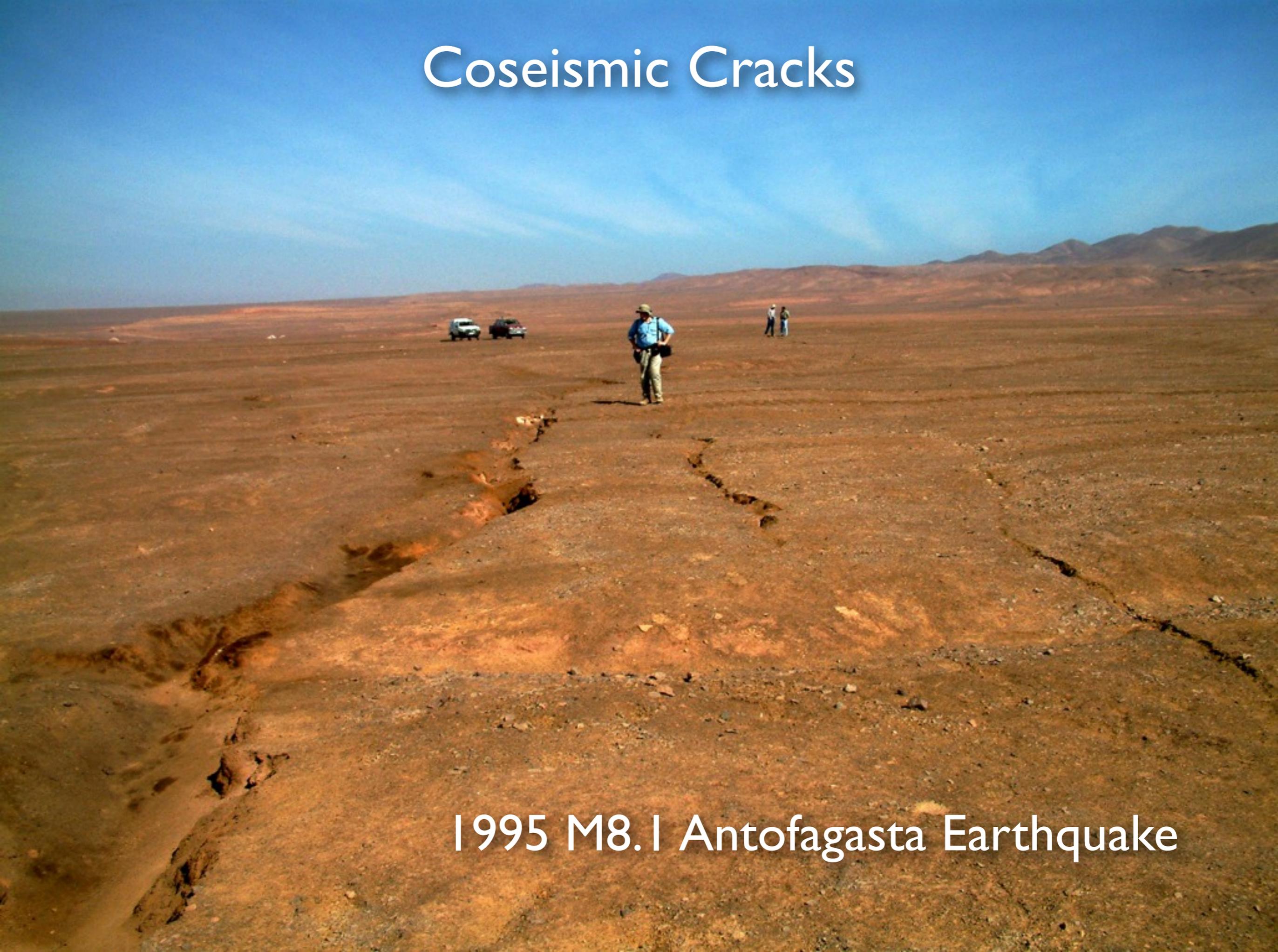
500 m



Crack in Bedrock



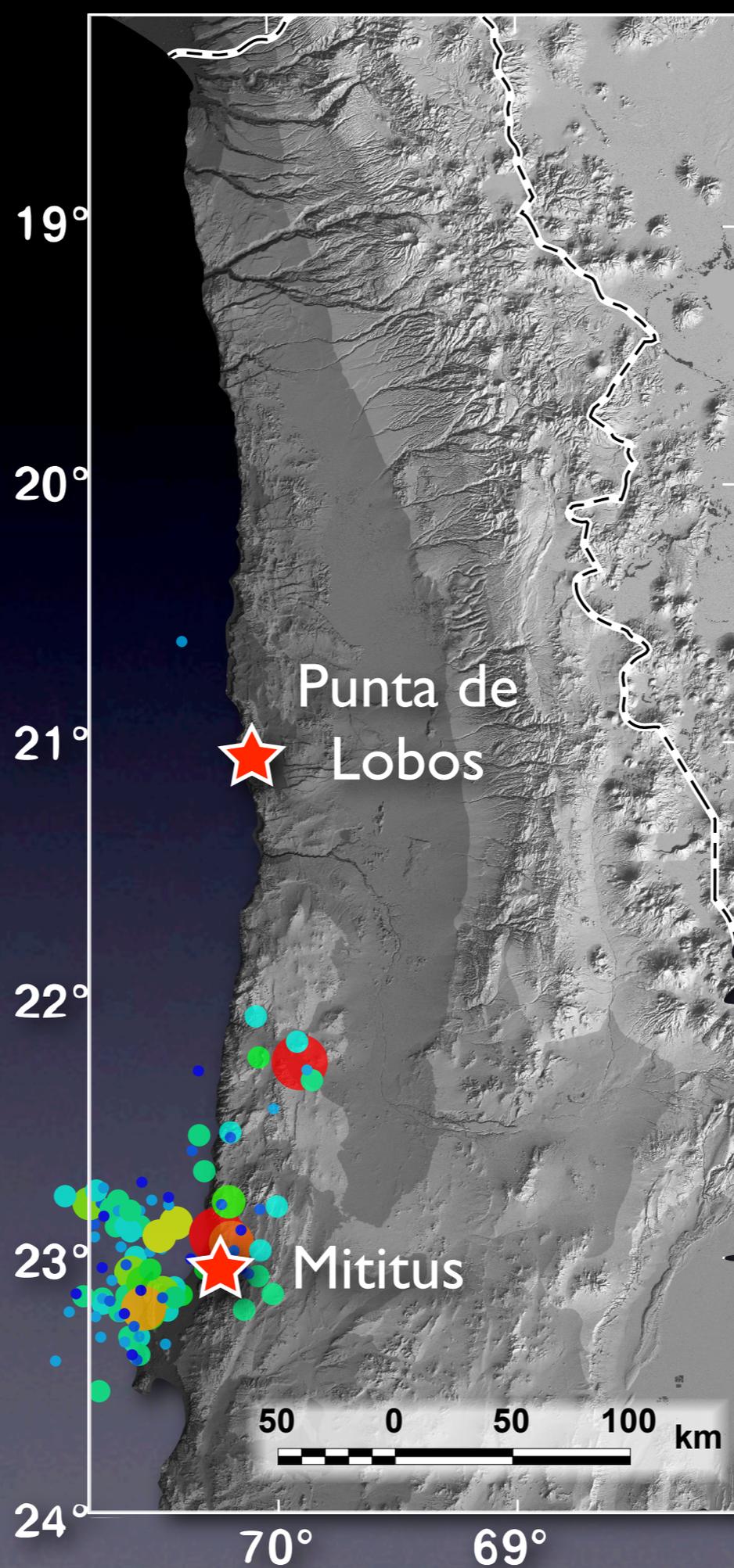
Coseismic Cracks



1995 M8.1 Antofagasta Earthquake

Crack Study Areas

2007 M_w 7.7
Tocopilla
aftershocks



Coseismic Cracks — M7.7 Tocopilla 2007



Tocopilla Earthquake — Crack Reactivation

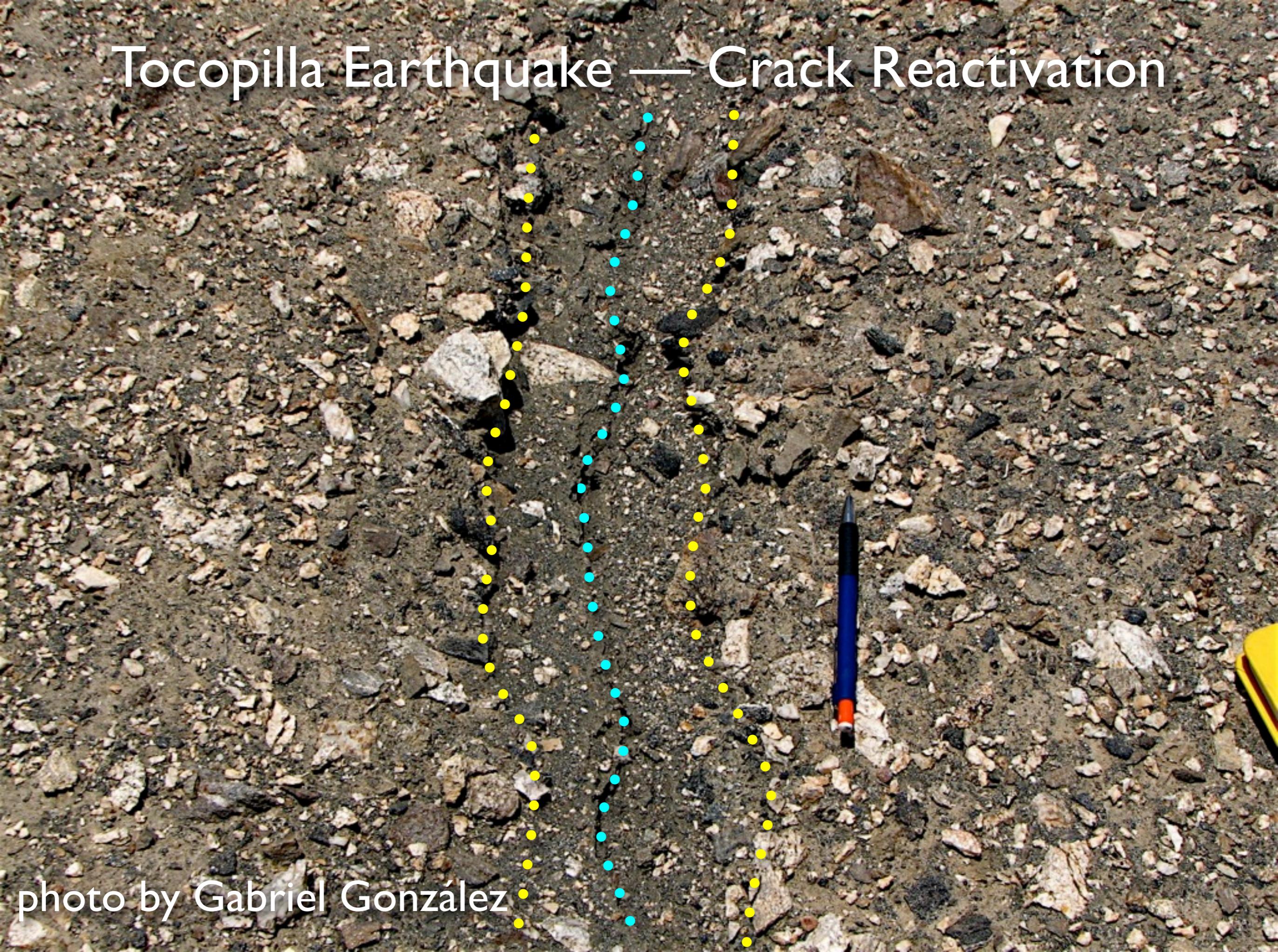
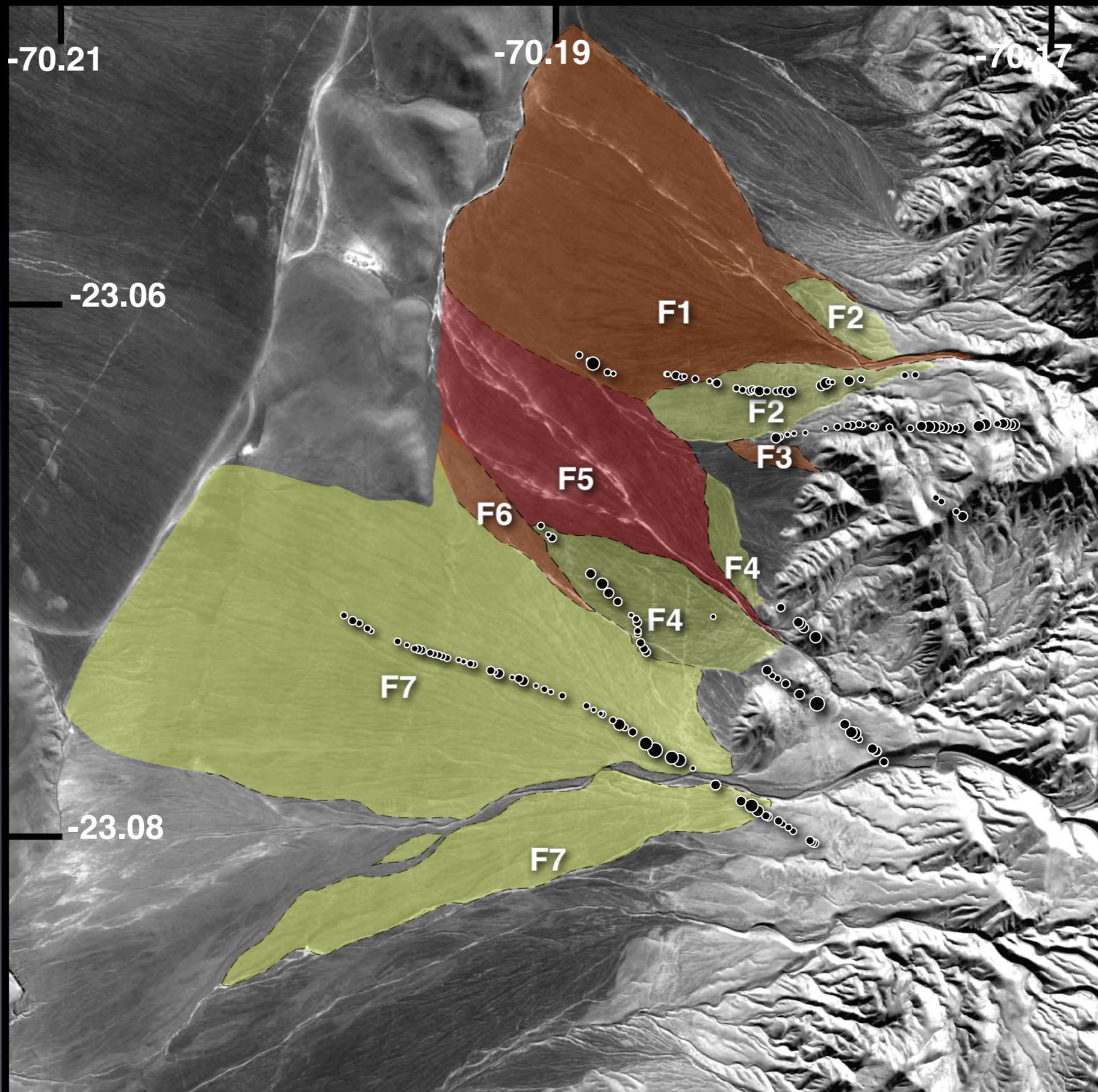


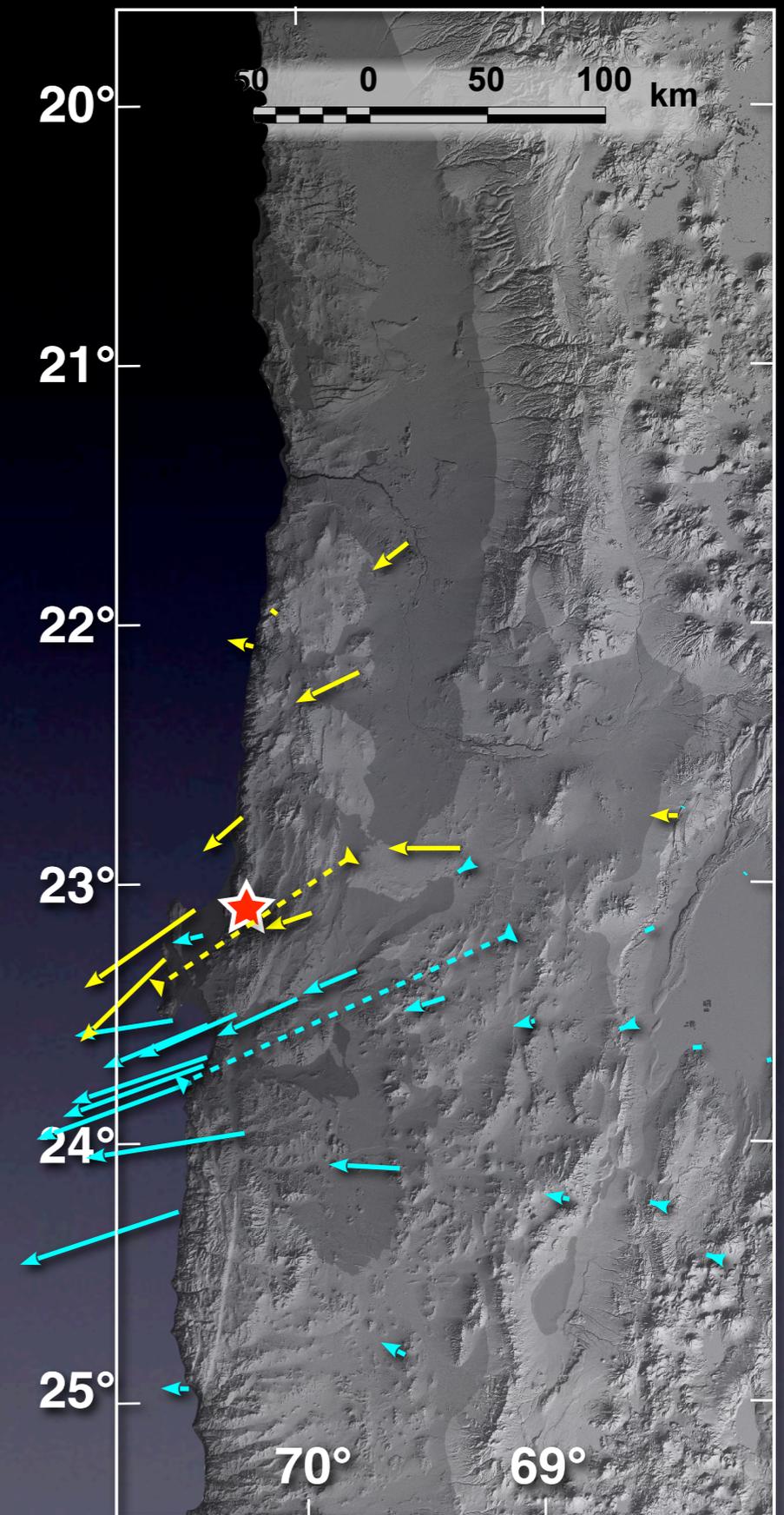
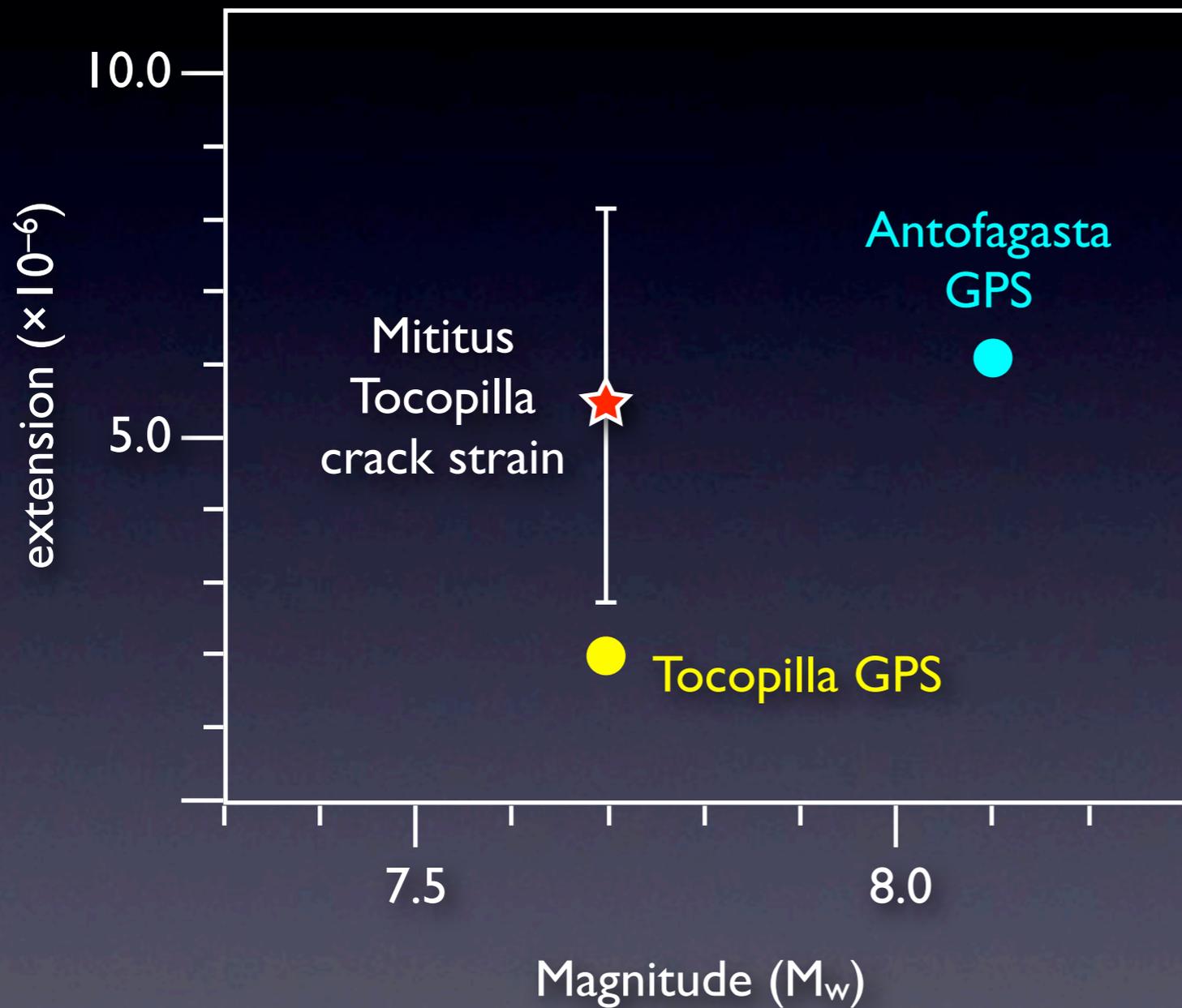
photo by Gabriel González

Mititus Area — Northern Part

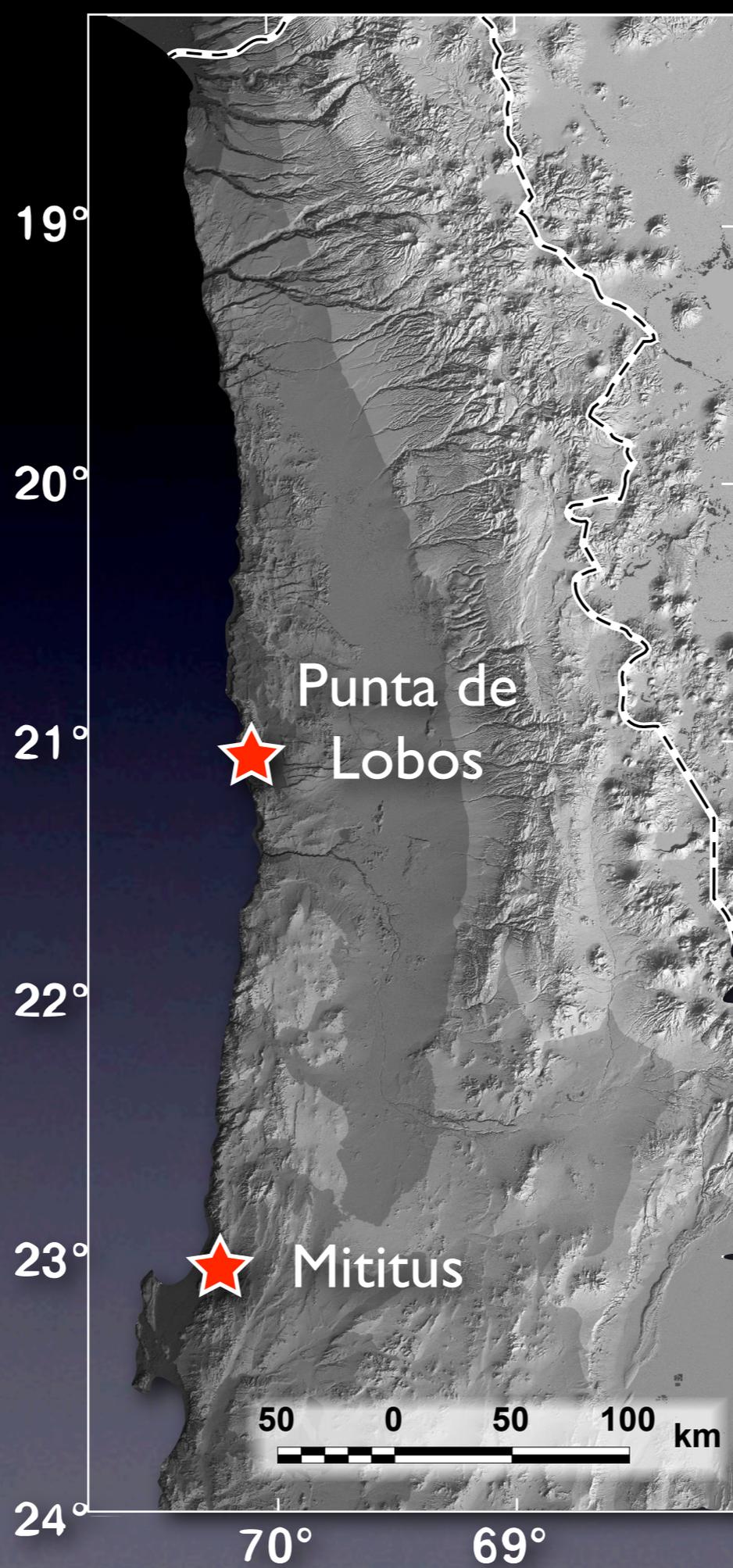


Baker (2012)

Coseismic Geodetic Strain & Crack Strain



Crack Study Areas



0 200 400 600 800 1000 m

Punta de Lobos Fan



Punta de Lobos Fan





~200,000 yr surface

~800,000 yr surface

0 200 400 600 800 1000 m

Punta de Lobos Fan

Baker et al.
(submitted)

Bajada

F2

F1

F2

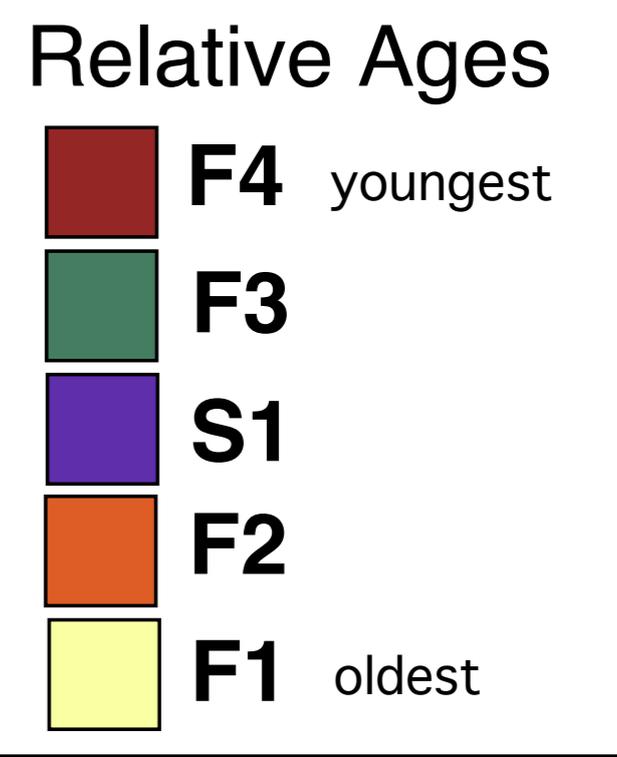
700

Bajada

F4

F3

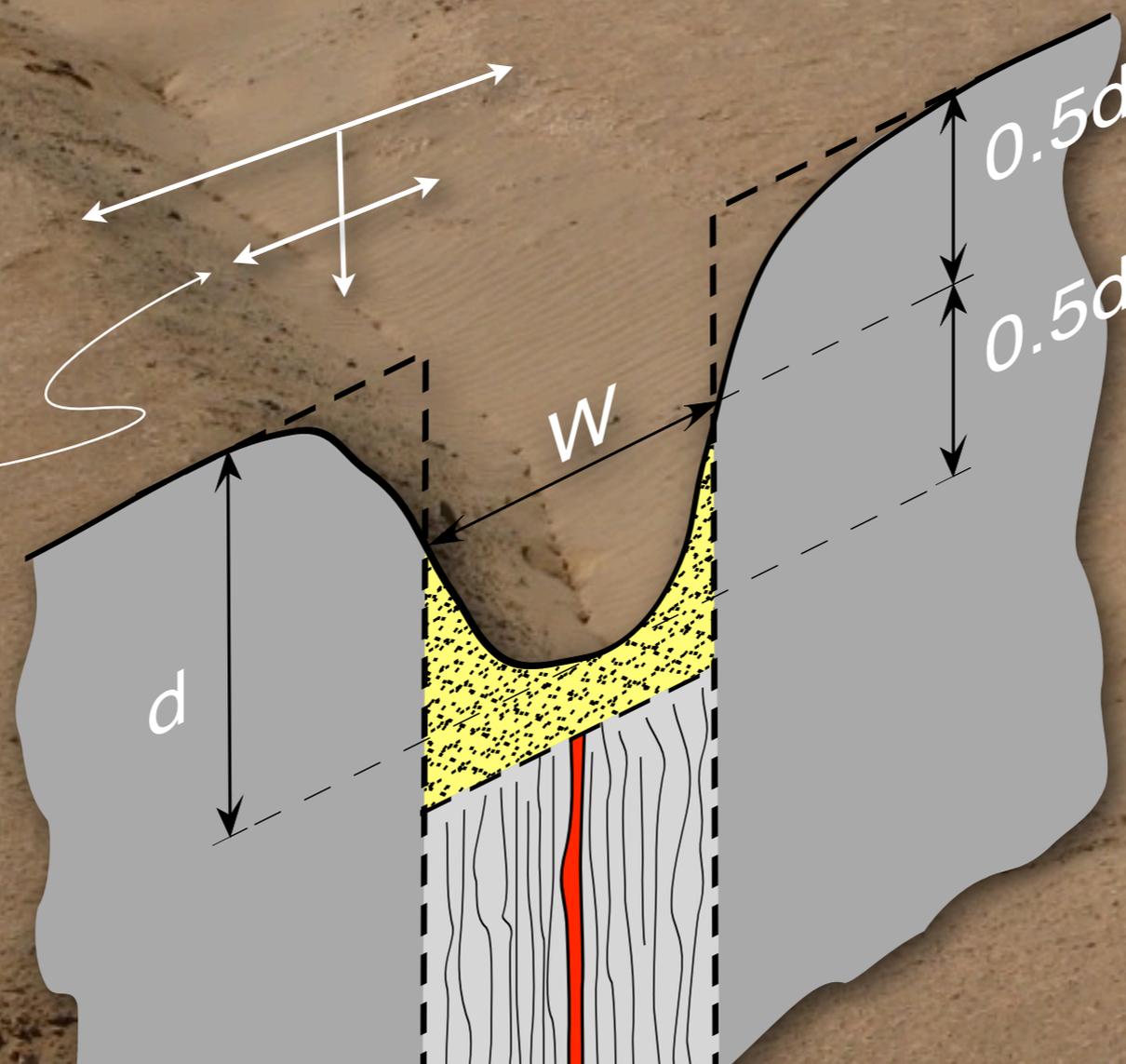
S1



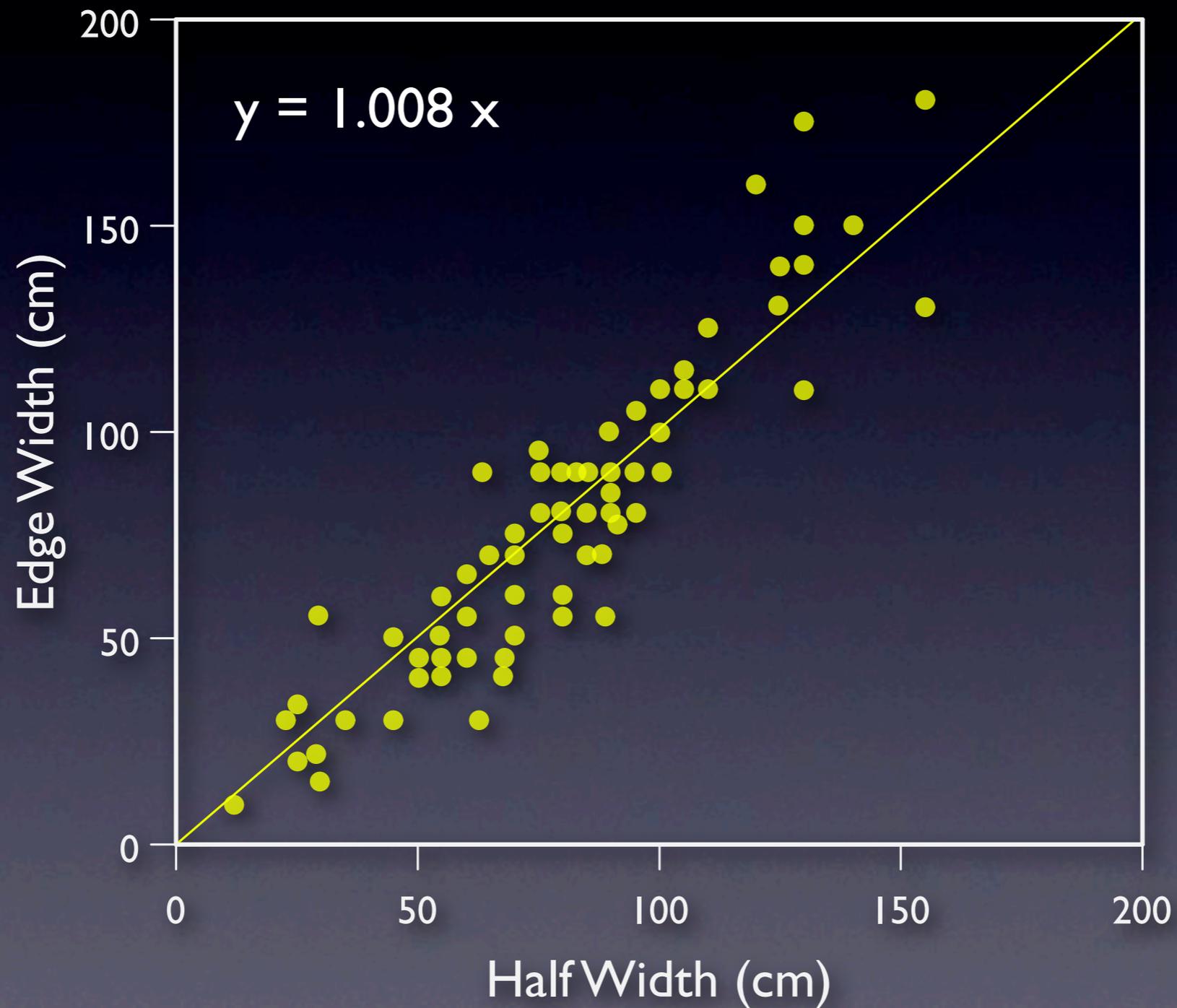
800

Estimating Crack Opening

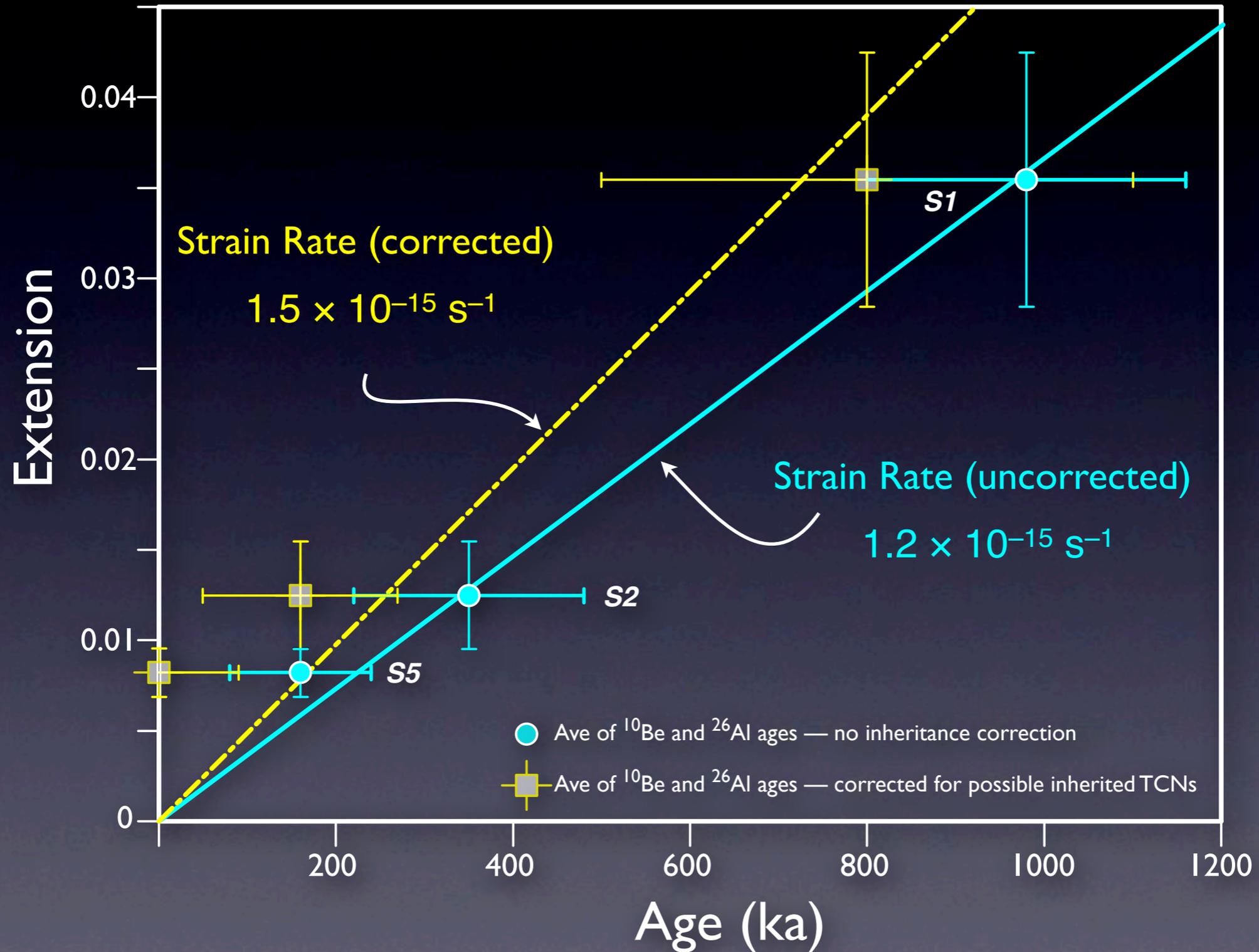
width at $\frac{1}{2}$
the depth



Estimating Crack Width



Strain Rates due to Cracking



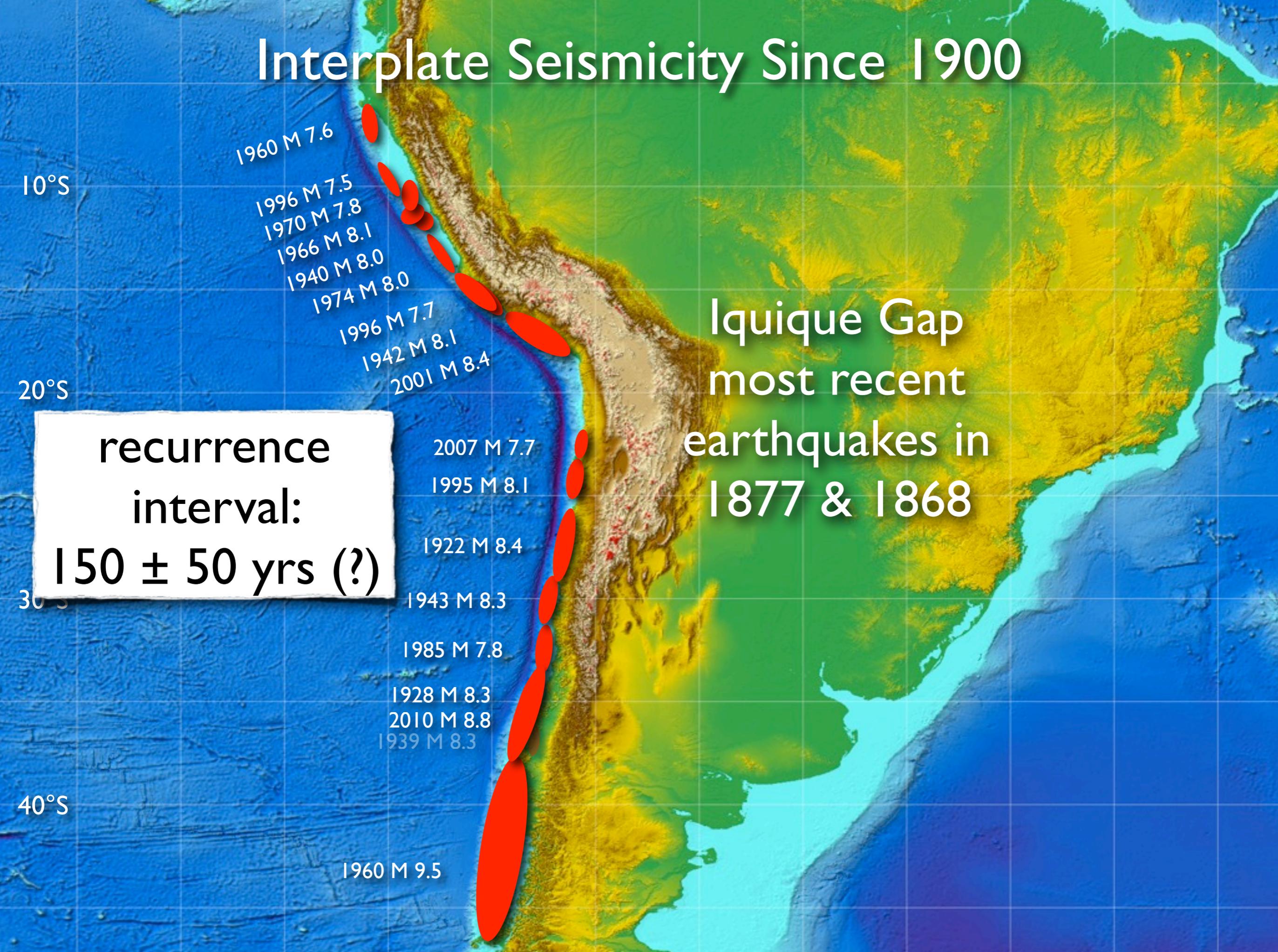
Interplate Seismicity Since 1900

10°S
20°S
30°S
40°S

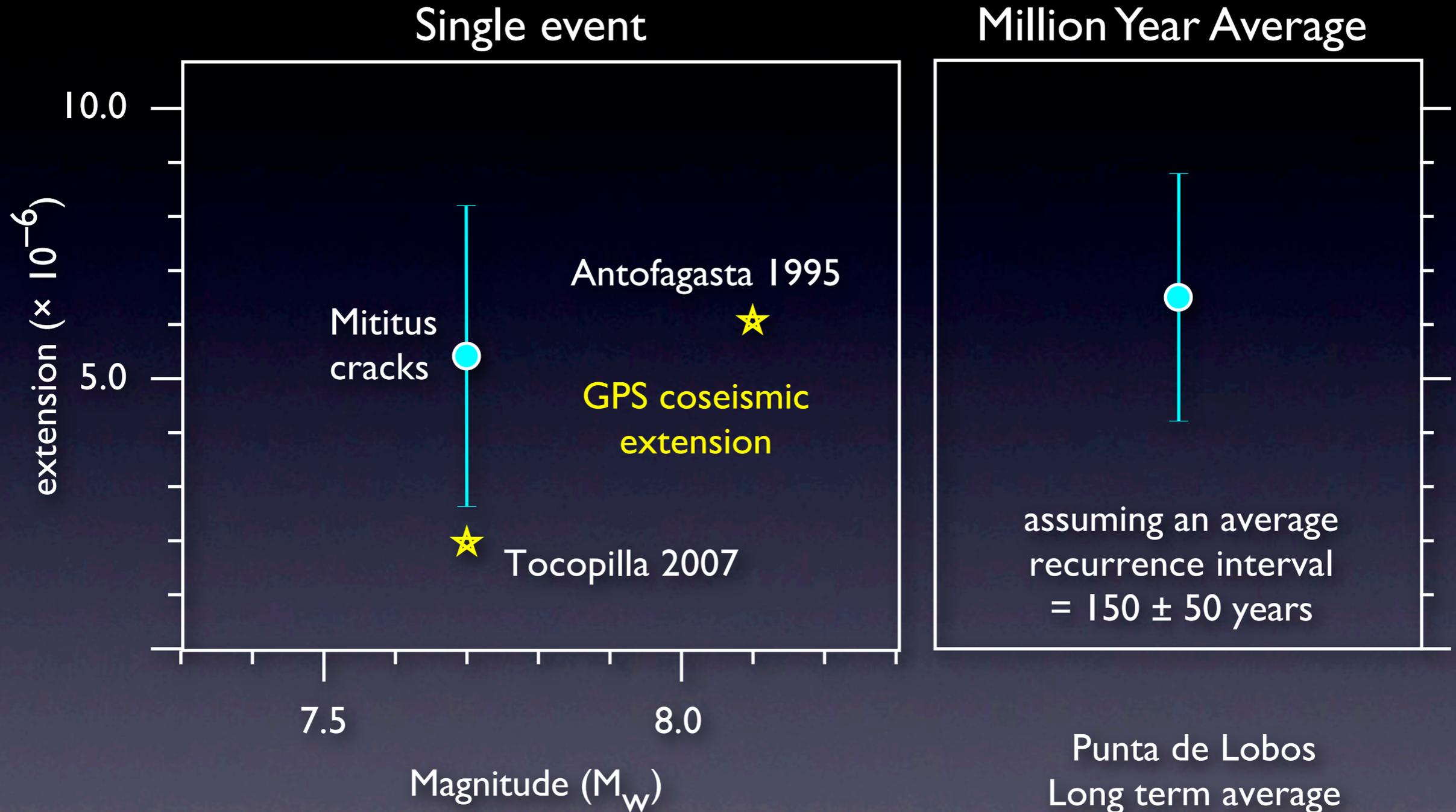
**recurrence interval:
150 ± 50 yrs (?)**

- 1960 M 7.6
- 1996 M 7.5
- 1970 M 7.8
- 1966 M 8.1
- 1940 M 8.0
- 1974 M 8.0
- 1996 M 7.7
- 1942 M 8.1
- 2001 M 8.4
- 2007 M 7.7
- 1995 M 8.1
- 1922 M 8.4
- 1943 M 8.3
- 1985 M 7.8
- 1928 M 8.3
- 2010 M 8.8
- 1939 M 8.3
- 1960 M 9.5

**Iquique Gap
most recent
earthquakes in
1877 & 1868**



Coseismic Geodetic Strain & Crack Strain

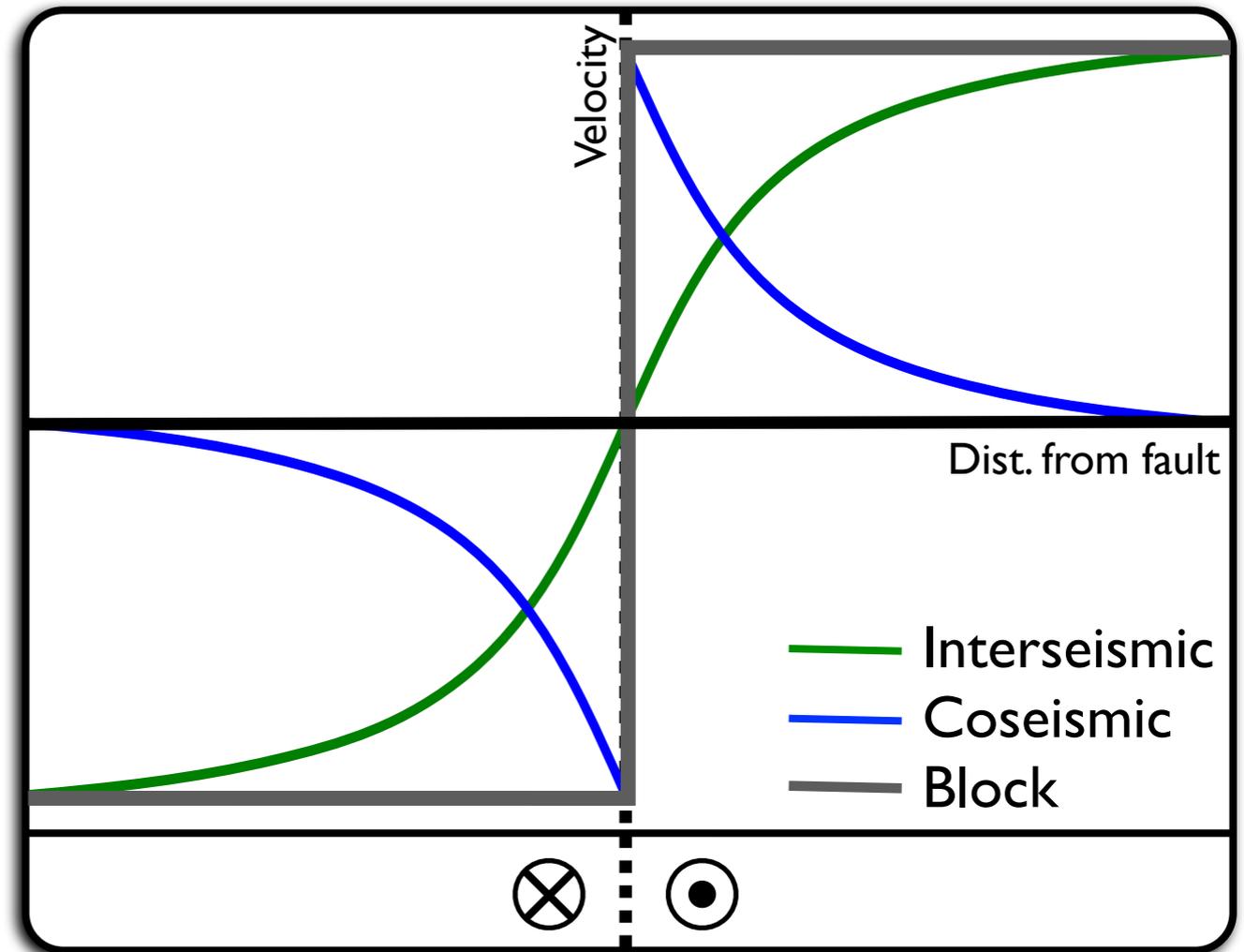
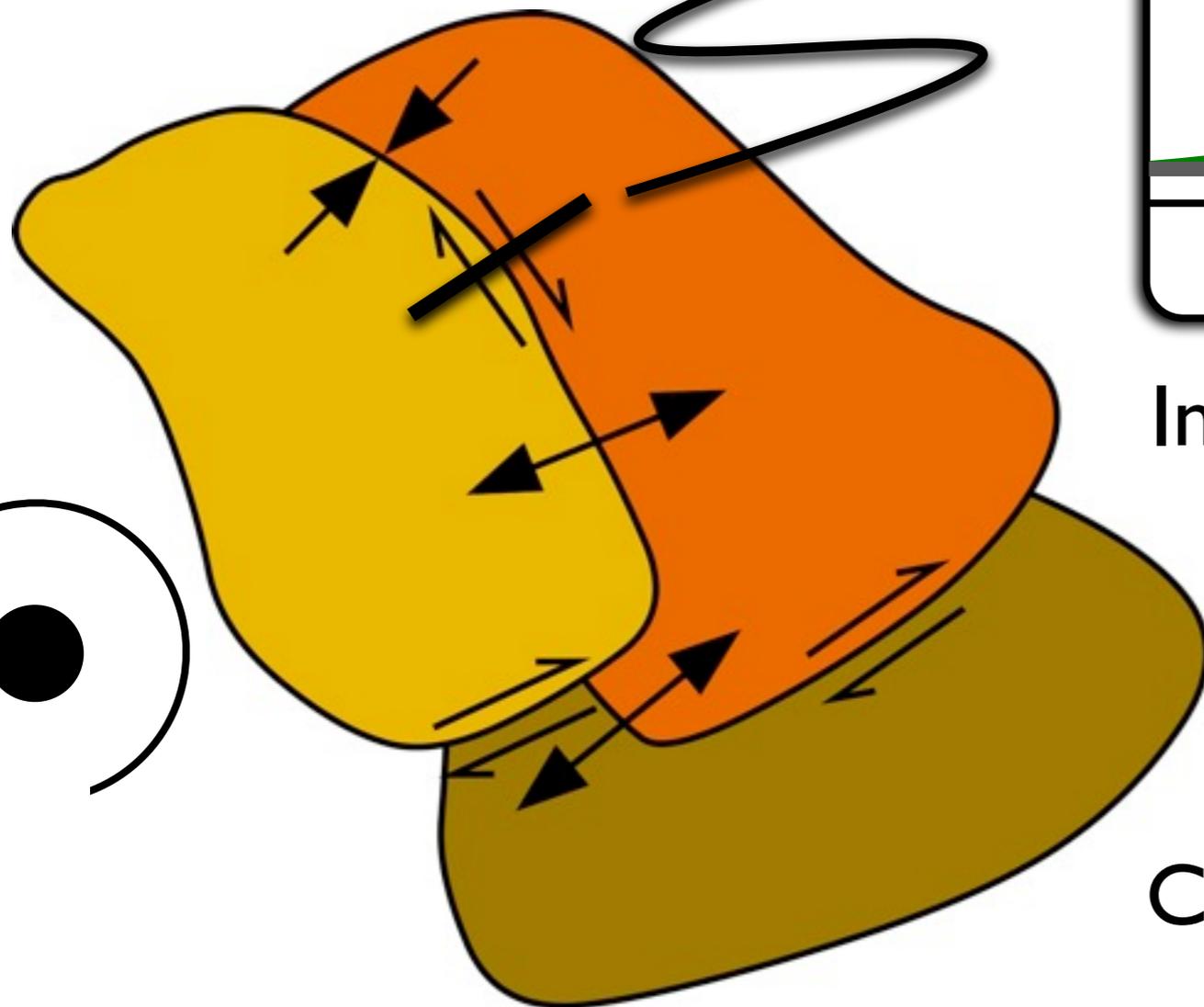


How much “elastic” rebound is permanent?

- Permanent crack strain is same order of magnitude as geodetic strain
- For a single event (Tocopilla 2007), permanent crack strain accounts for at very least $\sim 15\%$ of geodetic strain
- Both cracks and GPS sample the surface strain
- Implications for Reid model elastic rebound

Interseismic elastic block modeling

Block interactions described by rotation about Euler poles

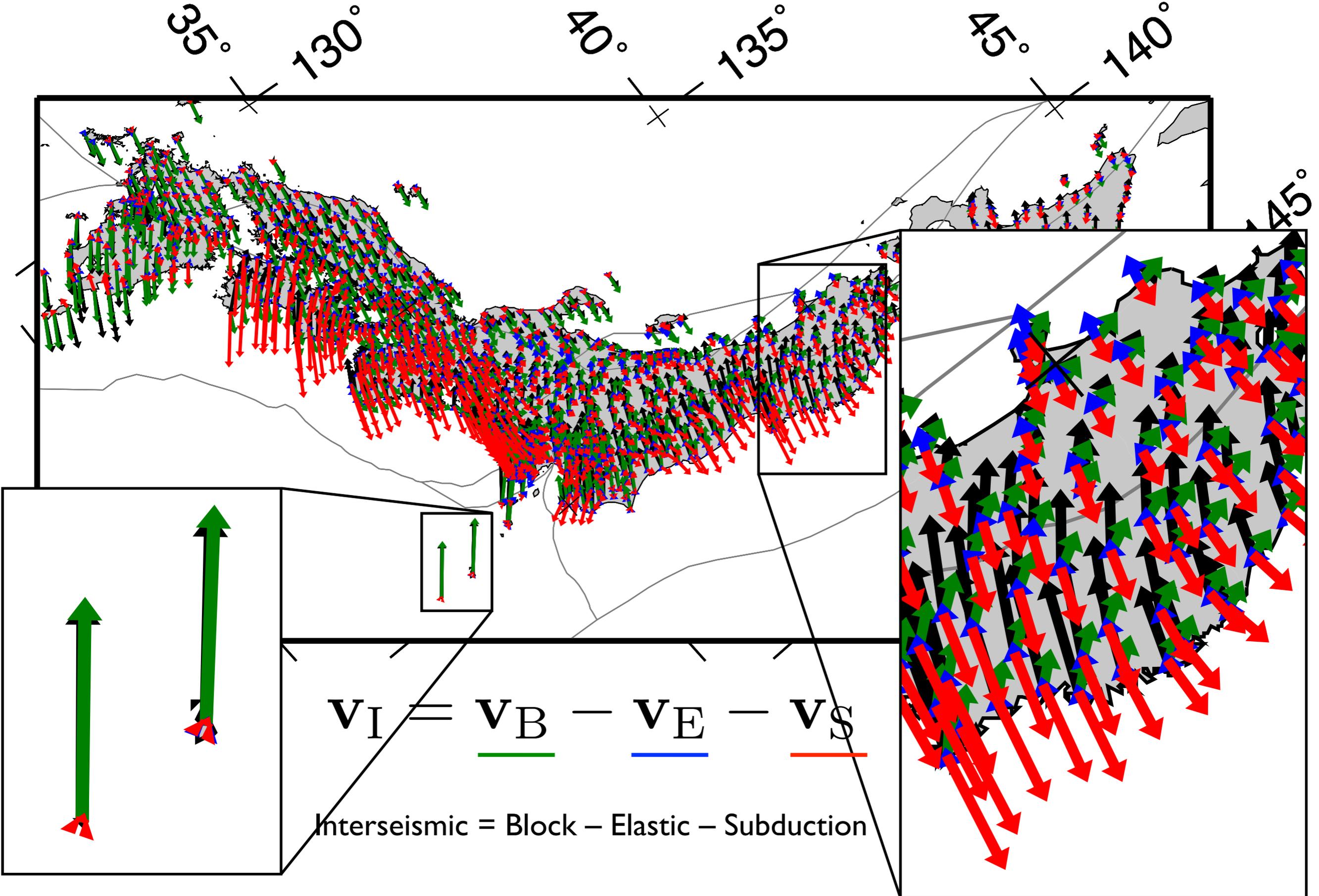


$$\text{Interseismic} = \text{Block} - \text{Coseismic}$$

Subtraction of coseismic:
Coseismic Slip Deficit

Consideration of block motion +
elastic effects → Block Model

Elastic block modeling: Velocity decomposition



Constructing the block geometry

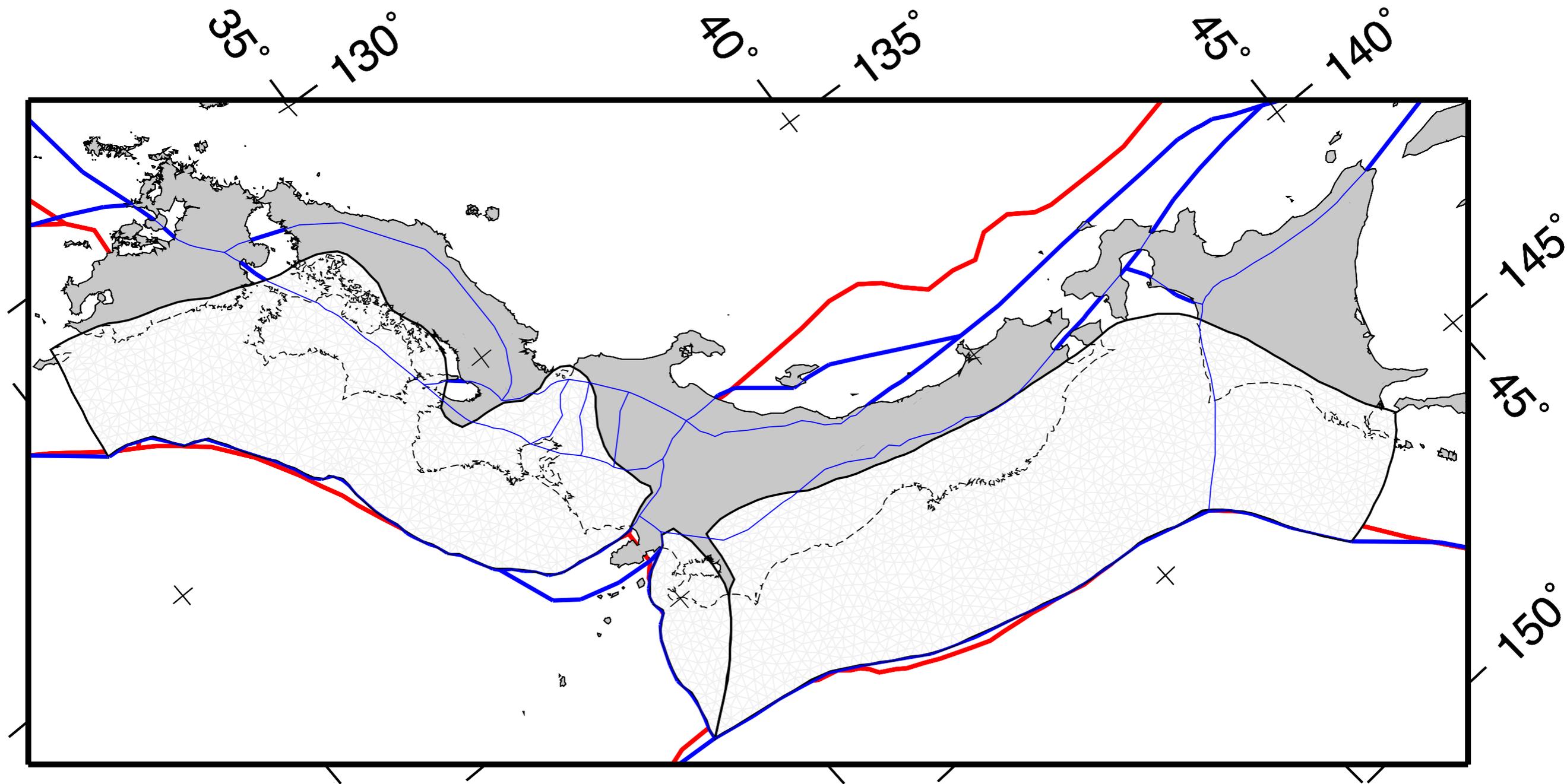
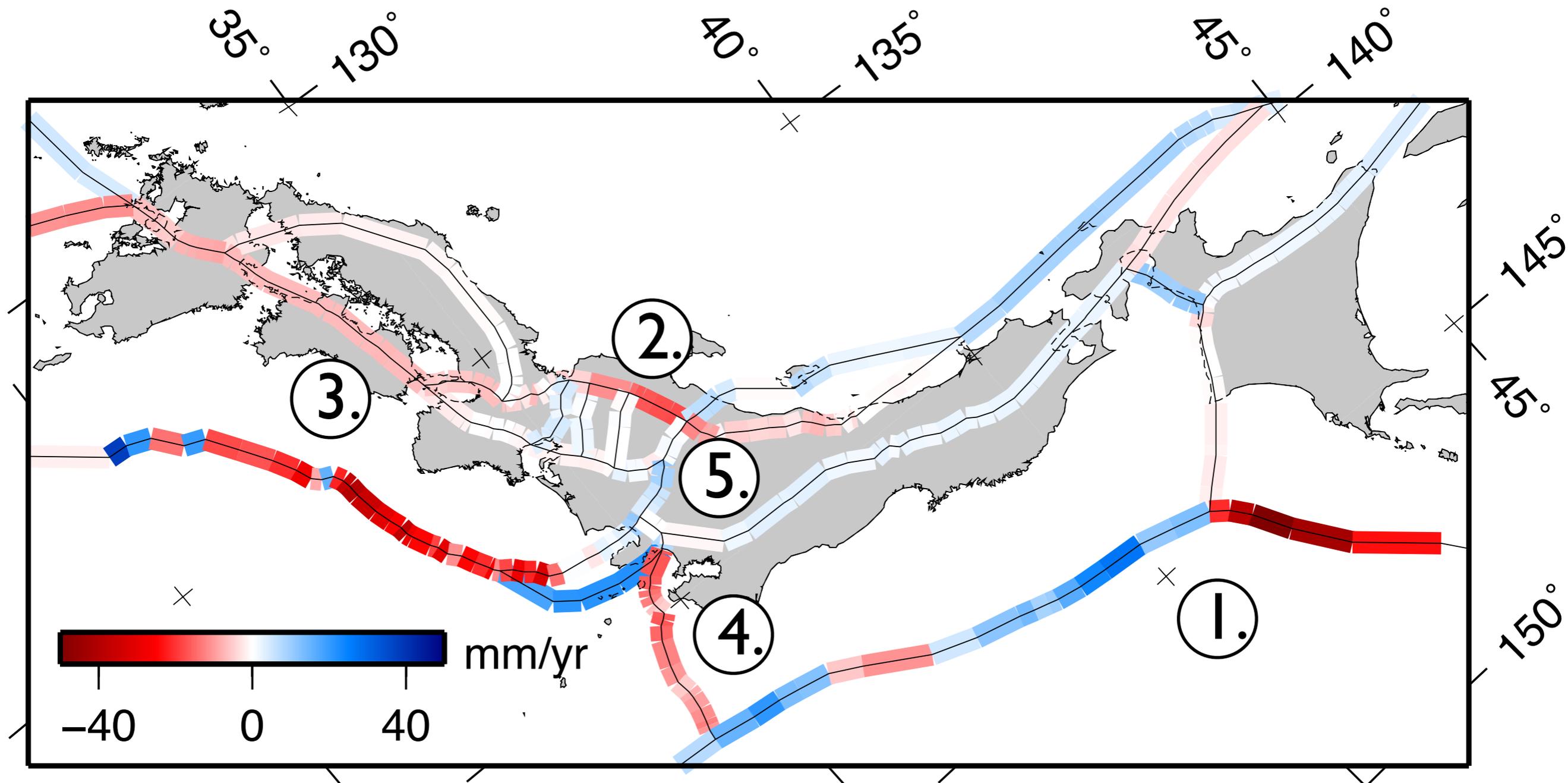


Plate boundaries → **Active fault traces** → **Block geometry**

e.g., Bird, *G³*, 2003

Digital Active Fault Map of Japan,
AIST online active fault database

Estimated strike-slip rates



Right-lateral

Left-lateral

1. Sign depends on strike of trench

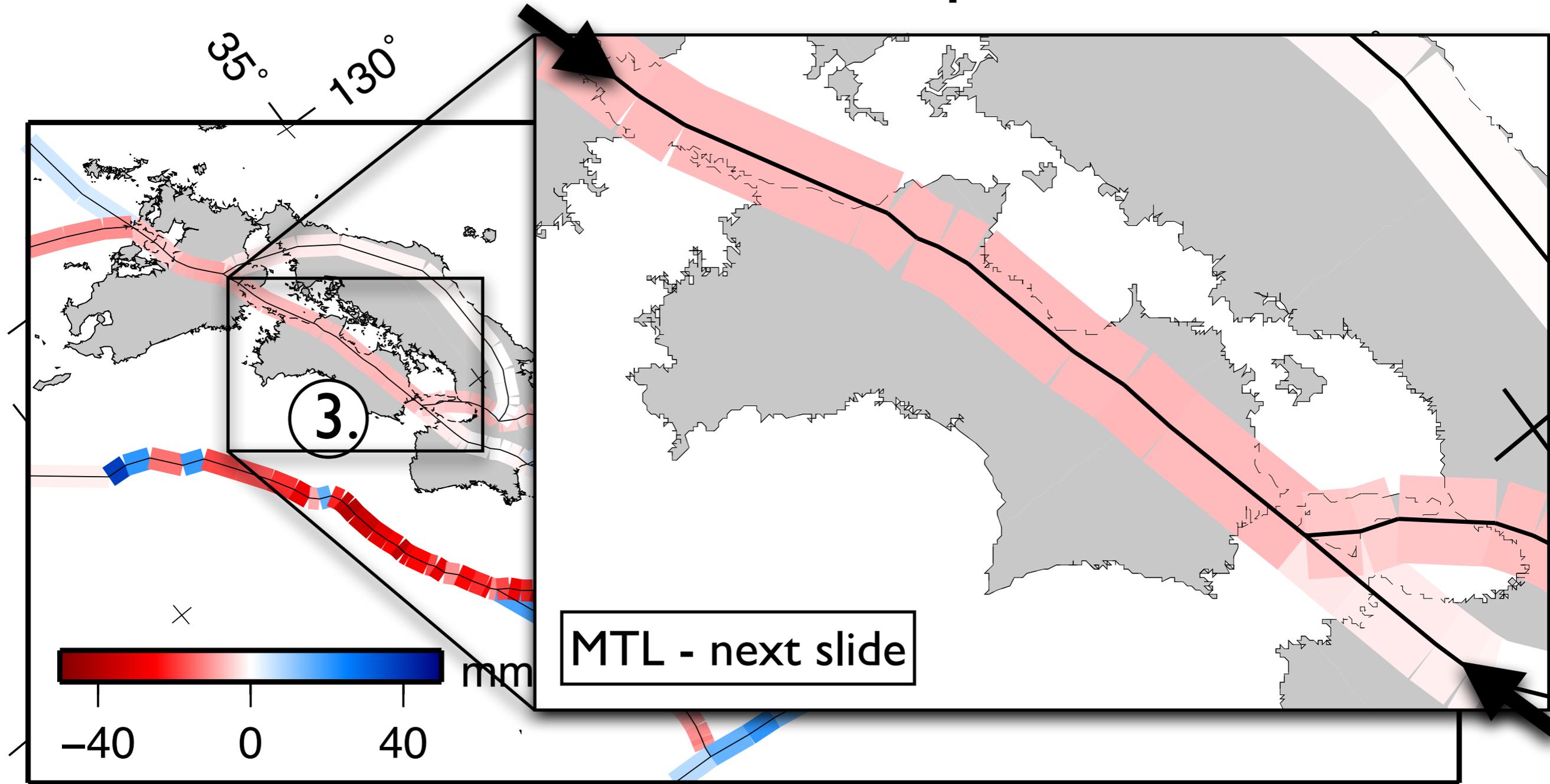
2. ~15 mm/yr R-L on NKTZ

3. ~7 mm/yr R-L on MTL, ~22 mm/yr at Nankai

4. ~17 mm/yr R-L at Sagami Trough

5. Up to 10 mm/yr L-L on ISTL

Estimated strike-slip rates

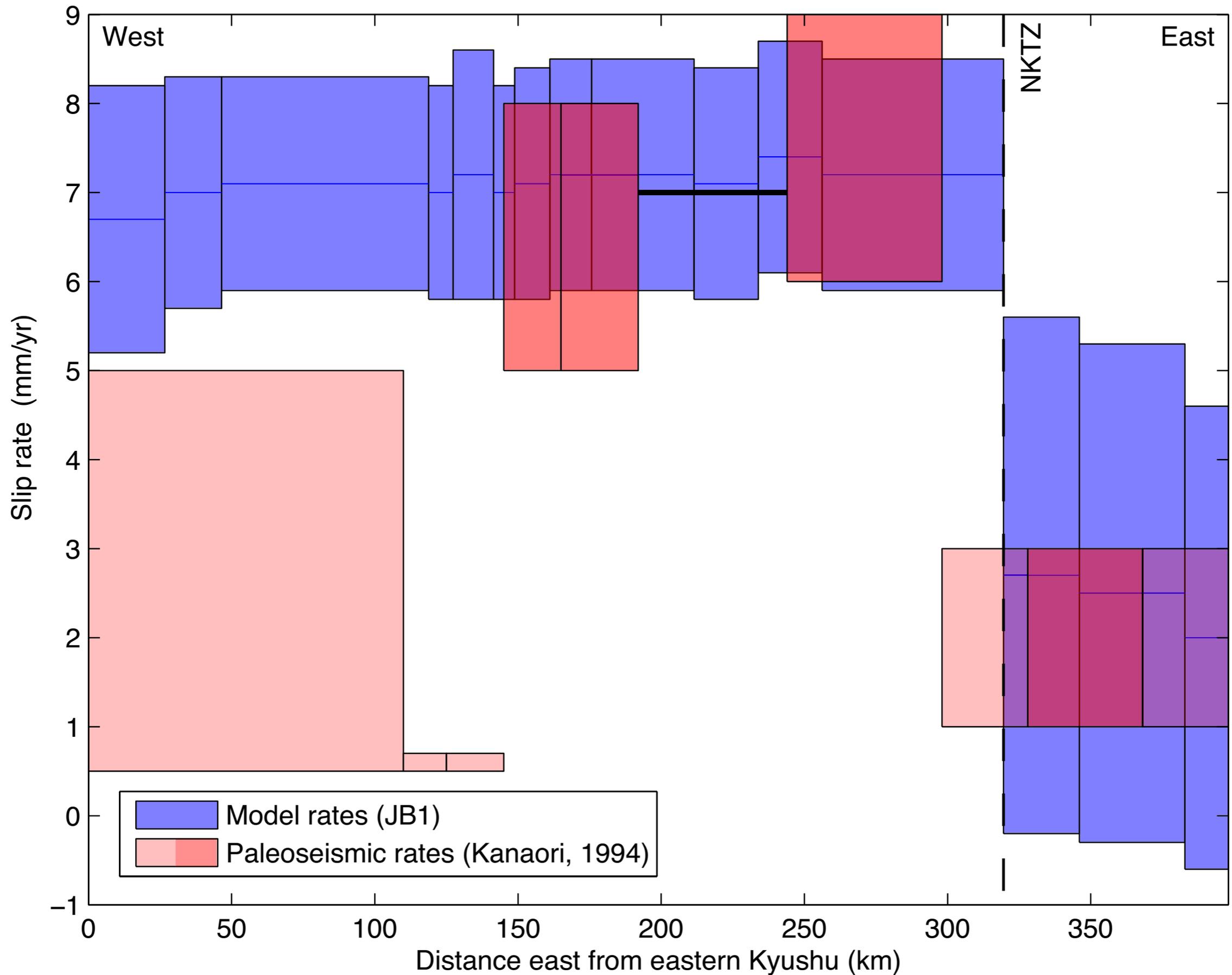


Right-lateral

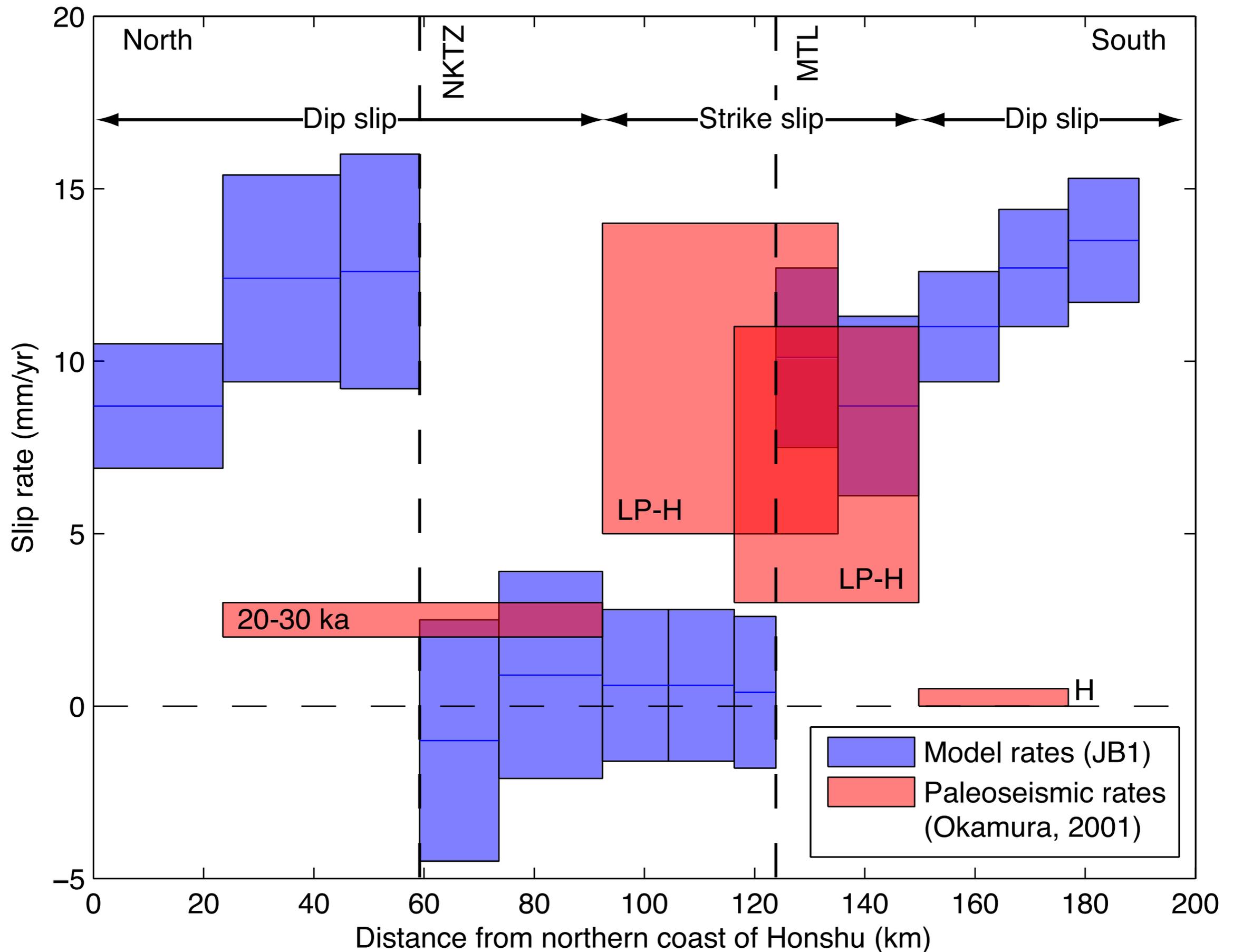
Left-lateral

1. Sign depends on strike of trench
2. ~15 mm/yr R-L on NKTZ
3. ~7 mm/yr R-L on MTL, ~22 mm/yr at Nankai
4. ~17 mm/yr R-L at Sagami Trough
5. Up to 10 mm/yr L-L on ISTL

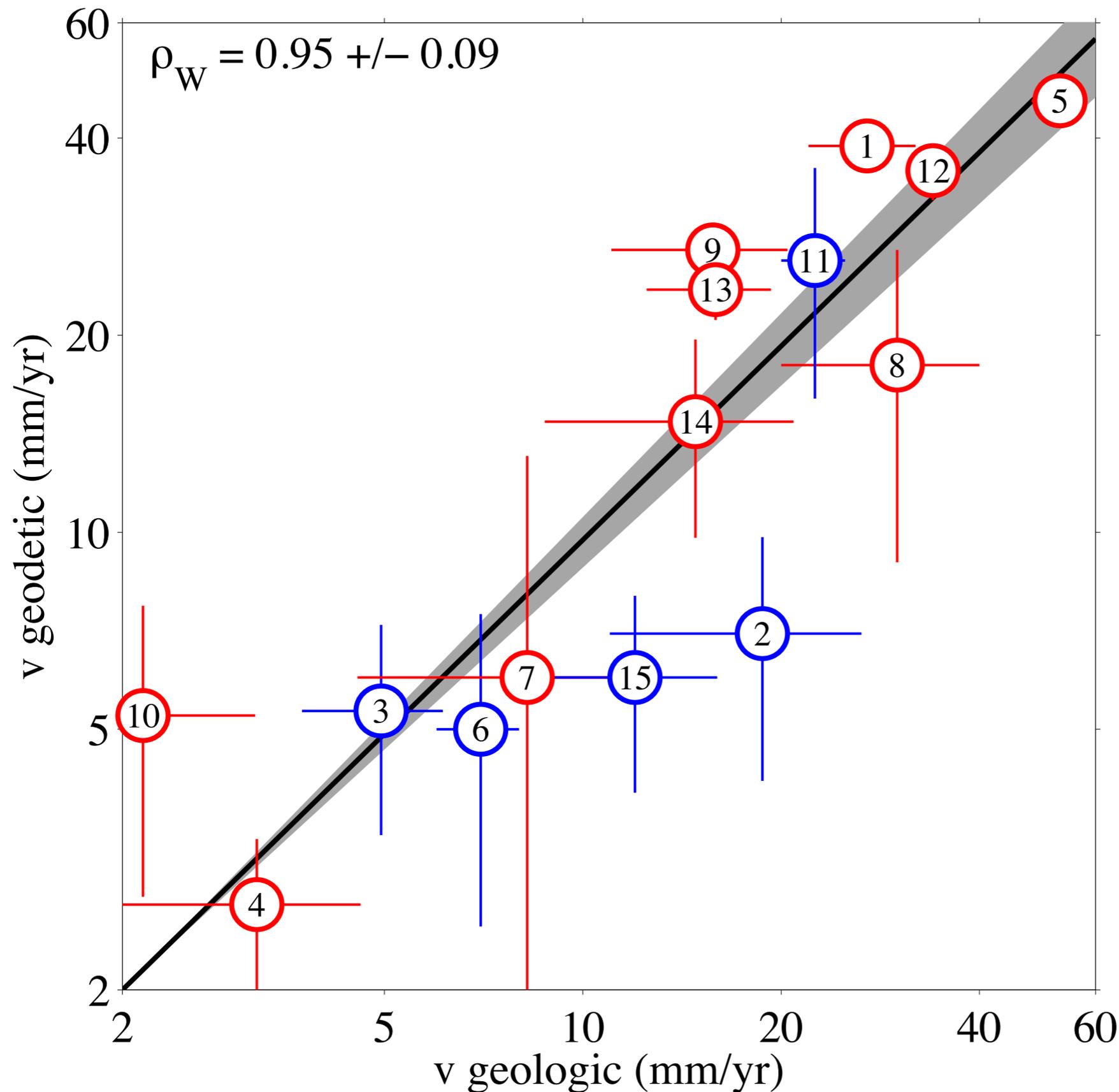
Fault slip through time: MTL



Fault slip through time: ISTL



Geodetic vs. geologic slip rates worldwide



- 1) Alpine
- 2) Altyn Tagh
- 3) Dead Sea
- 4) Elsinore
- 5) Fairweather
- 6) Garlock
- 7) Karakoram
- 8) SAF-Mojave
- 9) North Anatolian
- 10) Owens Valley
- 11) Philippine
- 12) SAF-Carrizo
- 13) SAF-Indio
- 14) San Jacinto
- 15) Haiyuan

Red = right-lateral
Blue = left-lateral

Consistency in deformation through time

- Examples of remarkable consistency in style and rate over times scales 10 yr – 10 Myr
- Discrepancies in rates bring about interesting questions:
 - Changing fault system geometry
 - Shifting locus of deformation
 - Transient rheologies
 - “Retrograde” coseismic deformation
 - Anomalous individual events that deviate from “average” behavior
- Elastic models are at best generalizations and slip models derived from them represent average behavior

Integrating geodesy and geology in courses

- Geodetic observations record active tectonics — discuss current events, newly formed/activated structures
- Geologic observations are of the end product of deformational processes
- Strain rate calculations are subject to length-scale issues and are better suited to interpreting regional deformation rather than individual fault processes
- Elastic models — for determining slip rates, slip areas, interseismic coupling, etc. — are oversimplified but often do a good job at interpreting geodetic observations
- Geologists can document the actual mechanisms by which geodetically observed strain occurs
- Big remaining question: how to integrate the seismic cycle over time to produce mountains?

Possible activities

- Calculate 1-D velocity gradients “by hand”
- Use StrainSim to calculate 2-D strain
 - Compare patterns of 2-D strain with patterns of faulting
 - Compare dilatation with uplift/subsidence
 - Compare relative magnitudes of strain with published fault slip rates
 - Compare principal strain axes with fault orientations
- Fit fault-parallel GPS velocities with screw dislocation model to estimate slip rate and locking depth